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[2,3] MCE (Maximum Model Distance)

[4]

HMM

(Principal Components Analysis)
(Linear Discriminant Analysis)

(Minimum Classification Error)

Aurora2

LDA PCA

MFCC

PCA

PCA

[5-7]

(HMM)

HMM

(Maximum Likelihood)

[1] EM (Expectation Maximization)

[8] LDA

(Discriminant Training)

(Maximum Mutual Information)

LDA PCA

[7]

PCA

LDA

PCA LDA

Kernel [12] Kernel LDA [9-11] Heteroscedastic LDA
[6] DCT [13,14] PCA

[19]

(Large-Margin MCE) LM-MCE

[15]

MCE

[21]

[16]

MCE

MCE [22]

Paliwal Wang [22]

[23]

MCE

() ()

$$d_{k,Add}(O, F) = -g_k(O, F) + \frac{1}{\eta} \log \left[\frac{1}{M-1} \sum_{i=1, i \neq k}^M \exp(g_i(O, F)\eta) \right] \quad ()$$

MCE

(LDA PCA)

$$d_{k,Div}(O, F) = \frac{\log \left[\frac{1}{M-1} \sum_{i=1, i \neq k}^M \exp(g_i(O, F)\eta) \right]}{\eta g_k(O, F)} \quad ()$$

MCE

([2]) η M

O

$g_i(O, \lambda_i)$

: ()

HMM λ_i

MCE

$$g_i(O, \lambda_i) = \log p(O | \lambda_i) \quad ()$$

(MCE)

() ()

MCE

[17,18]

() HMM

MCE

MCE

[2]

$$l_k(O, F) = \frac{1}{1 + \exp(-\alpha d_k(O, F))} \quad ()$$

HMM

)

MCE

(

α () ()

$d_k(O, F)$

Gradient Probabilistic

[19]

Descent

$d_k(O, F)$

$l_k(O, F)$

MCE

$d_k(O, F)$

[20]

$l_k(O, F)$

MCE

: () O

$$L = \sum_{k=1}^M l_k(O, F) \quad ()$$

$$\frac{\partial d_{k,ADD}(O,F)}{\partial W} = -\frac{\partial g_k(O,F)}{\partial W} + \quad ()$$

$$\sum_{i=1, i \neq k}^M \left(\frac{\exp(g_i(O,F)\eta)}{\sum_{j=1, j \neq k}^M \exp(g_j(O,F)\eta)} \times \frac{\partial g_i(O,F)}{\partial W} \right)$$

() L

$$\frac{\partial d_{k,Div}(O,F)}{\partial W} = \quad ()$$

$$g_k^{-1}(O,F) \sum_{i=1, i \neq k}^M \left(\frac{\exp(g_i(O,F)\eta)}{\sum_{j=1, j \neq k}^M \exp(g_j(O,F)\eta)} \times \frac{\partial g_i(O,F)}{\partial W} \right)$$

$$- \frac{\partial g_k(O,F)}{\partial W} g_k^{-2}(O,F) \log \left[\frac{1}{M-1} \sum_{i=1, i \neq k}^M \exp(g_i(O,F)\eta) \right]^{1/\eta}$$

$$w_{n,iter} = w_{n,iter-1} - \beta \frac{\partial L}{\partial w_n} \quad ()$$

$$\mathbf{W}_{iter} = \mathbf{W}_{iter-1} - \beta \frac{\partial L}{\partial \mathbf{W}} \quad ()$$

$$\mathbf{W} \quad r \quad r \quad \mathbf{W} \quad iter$$

$$\frac{\partial g_j(O,F)}{\partial W} \quad () \quad ()$$

$$O = WX$$

: [8]

$$\frac{\partial g_j(O,F)}{\partial W} = \sum_{t=1}^T \delta(q_t - j) b_j^{-1}(o_t) \frac{\partial b_j(o_t)}{\partial W} = \quad ()$$

$$- \sum_{t=1}^T \delta(q_t - j) \sum_{m=1}^M \gamma_{jm}(o_t) [C_{jm}^{-1}(o_t - \mu_{jm}) x_t^T]$$

$\delta(\cdot)$ M $j = 1, 2, \dots, M$
 $t \quad x_t$ t HMM q_t Kronecker

$$b_j(o_t) \quad T \quad o_t = Wx_t$$

HMM

$j \quad o_t$

() MCE
 PCA LDA

\mathbf{W} MCE

$(d \leq n) \quad d \quad y \quad x \quad n$

\mathbf{W}

$\mathbf{W} \quad ()$

$$b_j(o_t) = \sum_{m=1}^M c_{jm} b_j(o_t) =$$

$$\frac{1}{(2\pi)^{n/2}} \sum_{m=1}^M \frac{c_{jm}}{|C_{jm}|^{1/2}} \exp\left(-\frac{1}{2}(o_t - \mu_{jm})^T C_{jm}^{-1}(o_t - \mu_{jm})\right) \quad ()$$

$$C_{jm} \quad n \quad m \quad j$$

$$j \quad c_{jm} \quad m \quad j$$

$$\gamma_{jm}(o_t) \quad m$$

$$\gamma_{jm}(o_t) = \frac{c_{jm} b_j(o_t)}{b_j(o_t)} \quad ()$$

$$\frac{\partial l_k(O,F)}{\partial W} = \frac{\partial l_k(O,F)}{\partial d_k(O,F)} \frac{\partial d_k(O,F)}{\partial W} \quad ()$$

$$O \quad () \quad l_k(O,F)$$

$$O = \{o_1, o_2, \dots, o_T\}$$

$$X = \{x_1, x_2, \dots, x_T\}$$

: [8]

$$\frac{\partial l_k(O,F)}{\partial d_k(O,F)} = \alpha_k(O,F) (1 - l_k(O,F)) \quad ()$$

$$() \quad () \quad ()$$

()

PCAMCE-D-opt

PCAMCE-D-Init PCAMCE-A-Init PCA

PCAMCE-A-opt

TEST TEST A MFCC

TEST C WER B

MFCC

PCA-based

	(WER)		
	A	B	C
MFCC	36.50	26.49	59.18
PCA	39.80	33.29	69.21
PCAMCE-A-Init	45.55	38.38	72.47
PCAMCE-D-Init	43.85	35.03	69.98
PCAMCE-A-opt	38.25	27.42	57.89
PCAMCE-D-opt	36.53	27.50	57.48

MCE LDA

LDA

MFCC MCE

LDAMCE-D- LDAMCE-A-opt LDAMCE-D-opt LDA

() LDAMCE-A-Init Init

LDA-based

	(WER)		
	A	B	C
MFCC	36.50	26.49	59.18
LDA	46.90	34.45	73.01
LDAMCE-A-Init	45.42	35.69	73.50
LDAMCE-D-Init	46.48	35.41	73.66
LDAMCE-A-opt	38.56	29.44	57.72
LDAMCE-D-opt	37.94	29.10	59.11

()

LDAMCE A

LDAMCE A Init LDA LDAMCE D opt opt

LDAMCE D Init

% Test C % Test B % Test A

MFCC Test C

j $b_{jm}(o_t)$

() () () m o_t

() () ()

$\frac{\partial d_k(O, F)}{\partial W}$ $\frac{\partial d_k(O, F)}{\partial W}$

() () ()

W LDA PCA

()

Aurora2

MFCC

()

MCE

PCA

PCA

MCE

PCAMCE-A-opt PCAMCE-D-opt PCA MFCC

PCAMCE-A-Init PCAMCE-D-Init

()

(

)

MCE-A	()	MCE
MCE-D	()	MCE
PCAMCE-A-Init	PCA	W
PCAMCE-D-Init	PCA	W
PCAMCE-A-opt	PCA	MCE-A
PCAMCE-D-opt	PCA	MCE-D
LDAMCE-A-Init	MCE-A	LDA W
LDAMCE-D-Init	MCE-D	LDA W
LDAMCE-A-opt	LDA	MCE-A
LDAMCE-D-opt	LDA	MCE-D

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MFCC Test B Test A

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