

# Assessment of robust capacity utilisation in railway networks

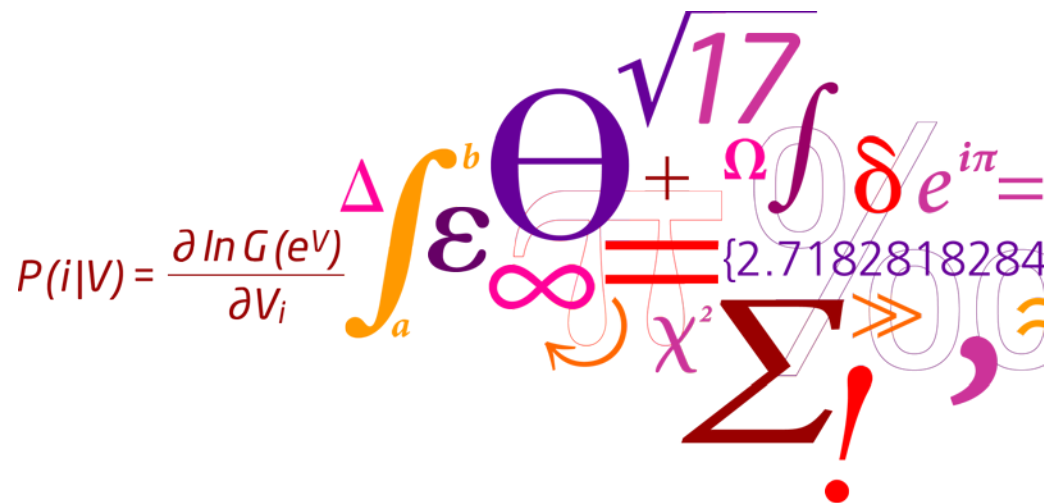
*Lars Wittrup Jensen*

RobustRailS Mini Conference 2015

RobustRailS

DTU Transport  
Department of Transport

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$$P(i|V) = \frac{\partial \ln G(eV)}{\partial V_i} \int_a^b \varepsilon \Theta^{\sqrt{17}} + \Omega \int \delta e^{i\pi} = \{2.7182818284\} \chi^2 \Sigma !$$


# Agenda

- 1) Introduction to WP 3.1 and PhD project
- 2) Model for measuring capacity consumption in railway networks
  - a) Motivation
  - b) Deterministic method
  - c) Stochastic method
  - d) Case
  - e) Excluding undesirable sequences

# Work package (and PhD) scope

- RobustRailS
  - Work package 3.1 on robustness in the railway operational process
- The goal is to develop methods to improve robustness of railway timetables/operation
- PhD project: **Robustness indicators and capacity models for railway networks**
  - Robustness indicators
  - Model for measuring capacity consumption in railway networks
    - Extension: measure capacity (as trains over a given time period)



# Work on robustness indicators

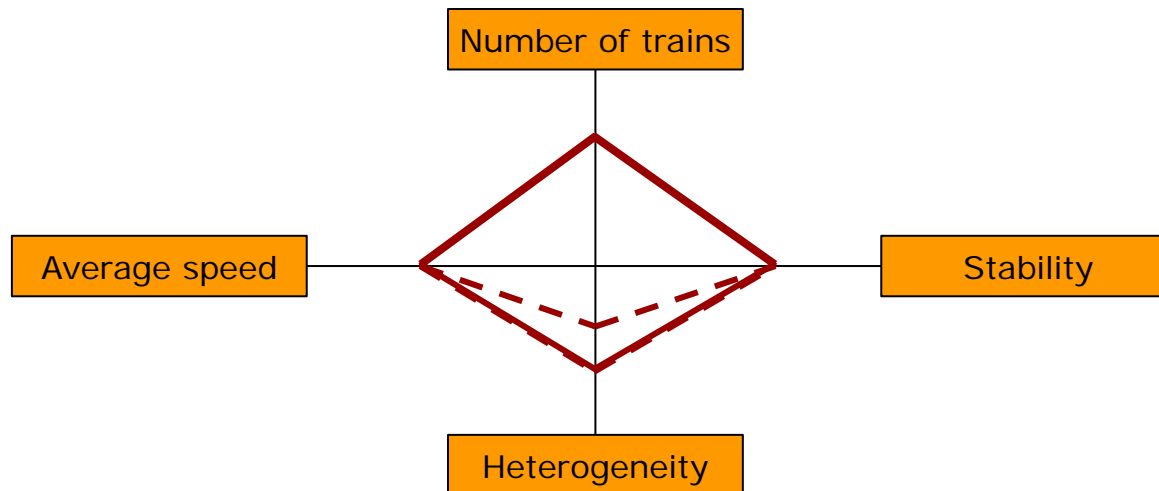
- Can robustness indicators be used in early planning phases and mathematical models instead of simulation which is time consuming?
- Identification and development of robustness indicators
- Comparison with simulation to determine ability to capture robustness
- Some robustness indicators linked well (complexities, UIC406 and train path risk profiles)
  - Some not (heterogeneity)
- Nothing can be concluded about the semantics of indicators

# Agenda

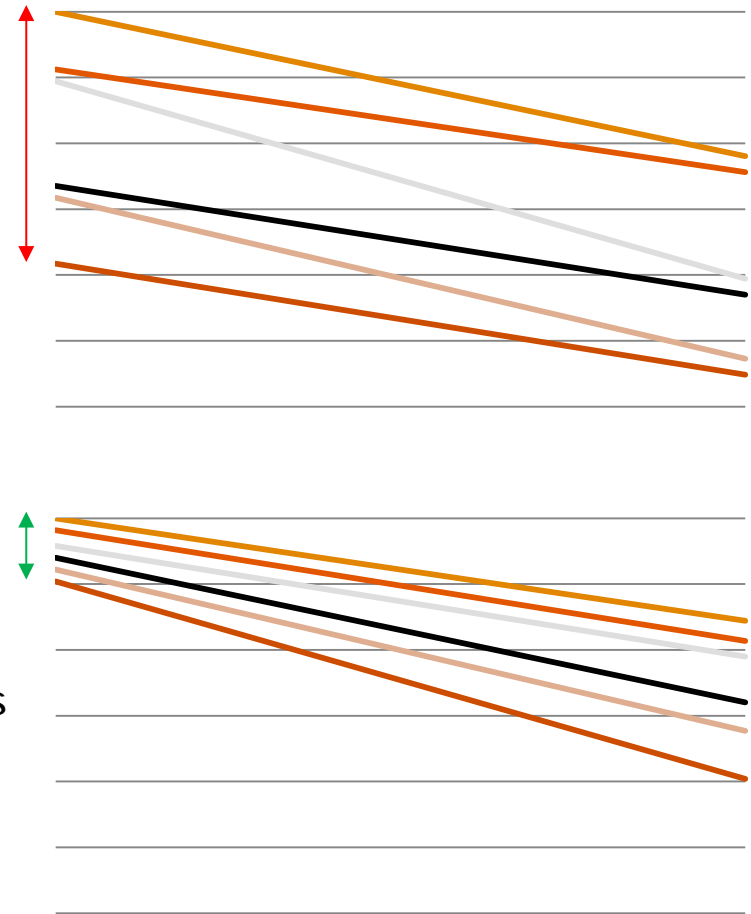
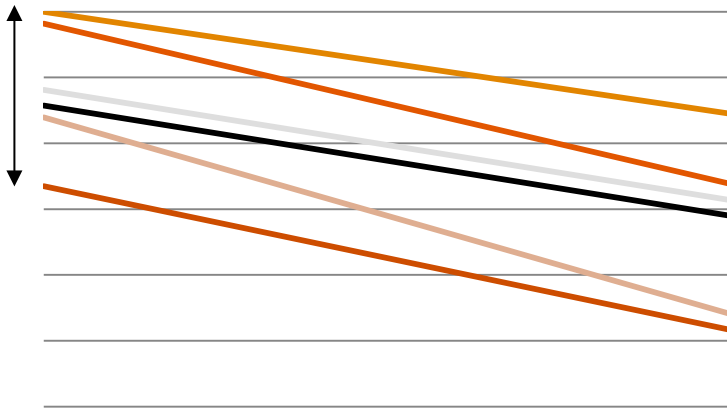
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# Motivation

- *What is the capacity consumed by a given set of trains?*
- A timetable is usually needed
- Usually only line sections are assessed (UIC406)
- Aim is to measure capacity consumption of a set of trains in a network
  - Only number of trains, train running times and headways are given
- Calculate the distribution of capacity rather than one single number
  - Deterministic capacity consumption (without delays)
  - Stochastic capacity consumption (with delays)

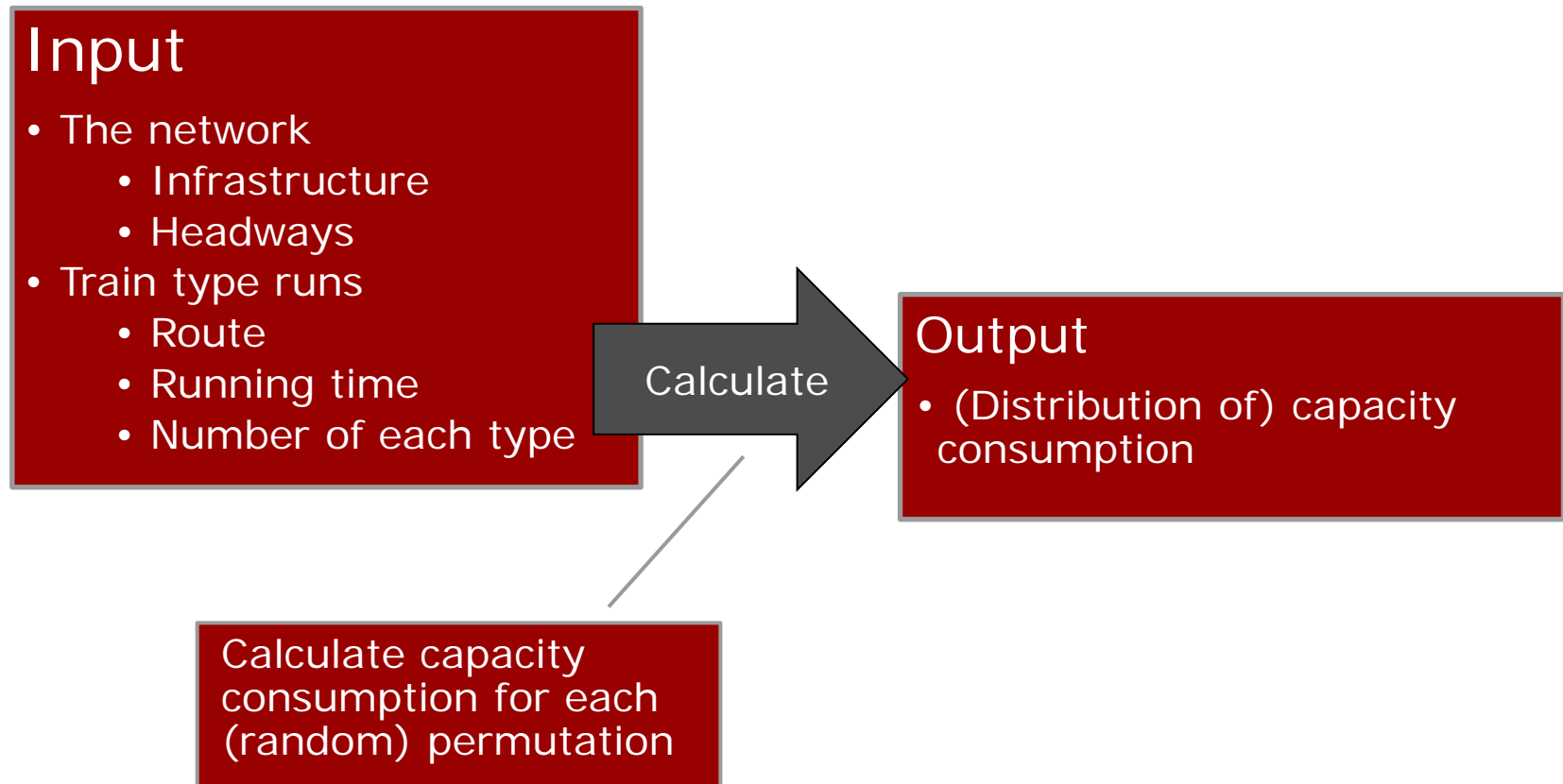


# How to mix trains - Heterogeneity



- $n!$  for acyclic timetables
- $(n-1)!$  permutations for cyclic timetables
- If more than 1 copy of a train type ( $k$ ):
  - $n!/(k_1!k_2!\dots k_m!)$   
(Multinomial coefficient)
- 16 trains (cyclic, 16 types)
  - 1.3 trillion permutations  
(1,307,674,368,000)

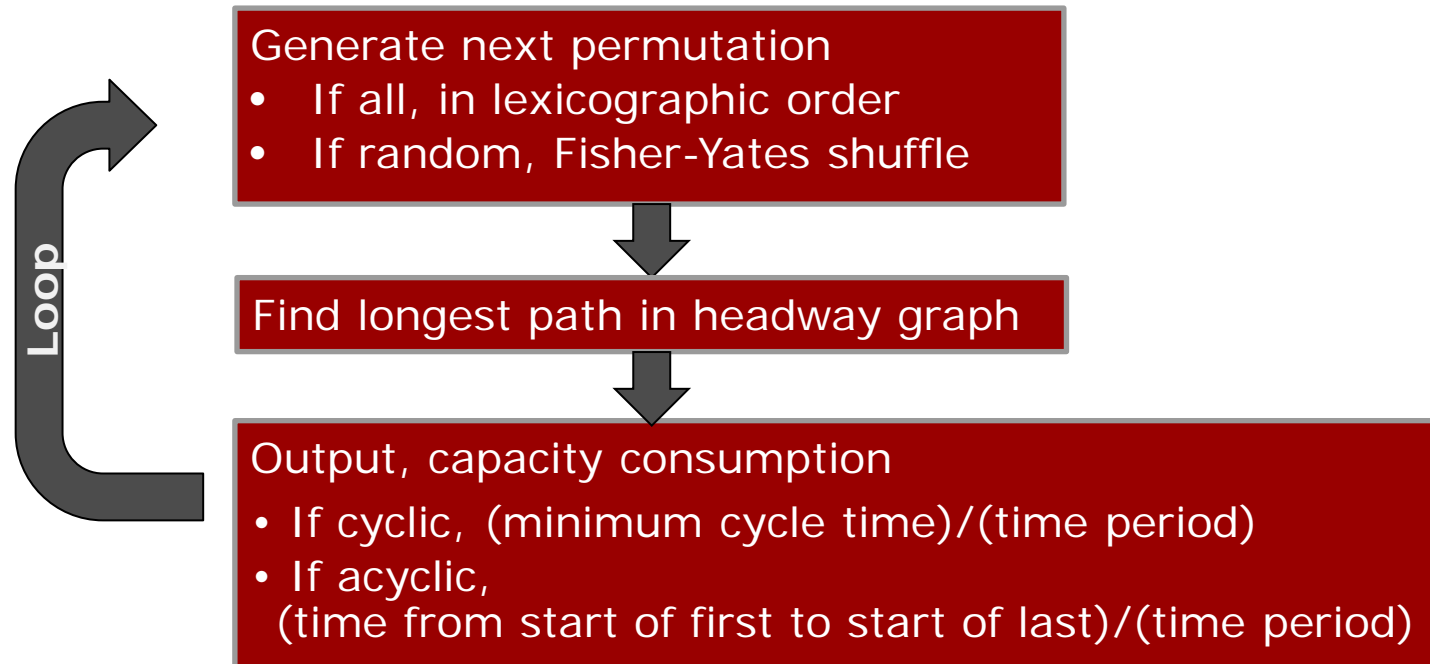
# Deterministic capacity consumption





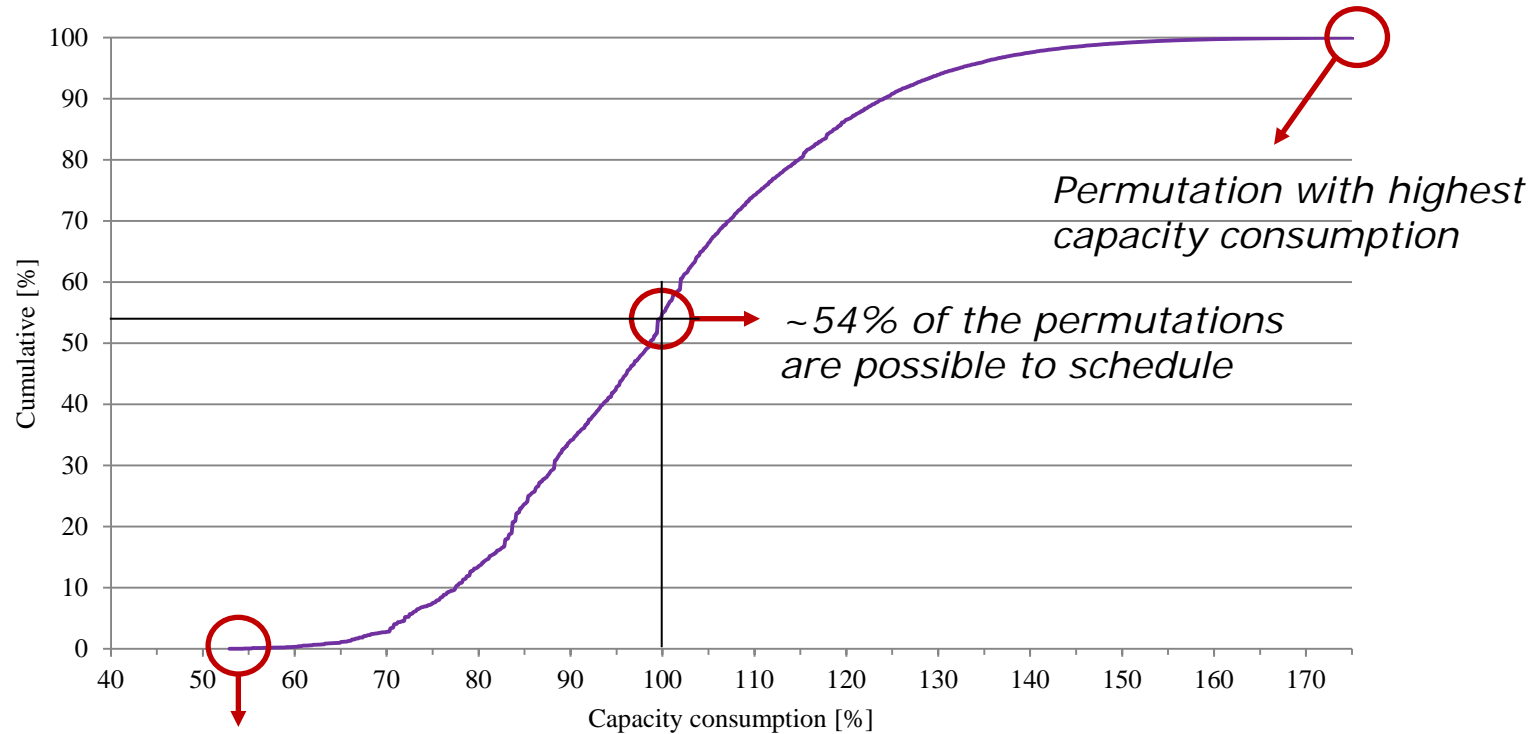
# Deterministic capacity consumption

Calculate capacity consumption for each (random) permutation



# Deterministic capacity consumption

- Output
  - Cumulative distribution of capacity consumption

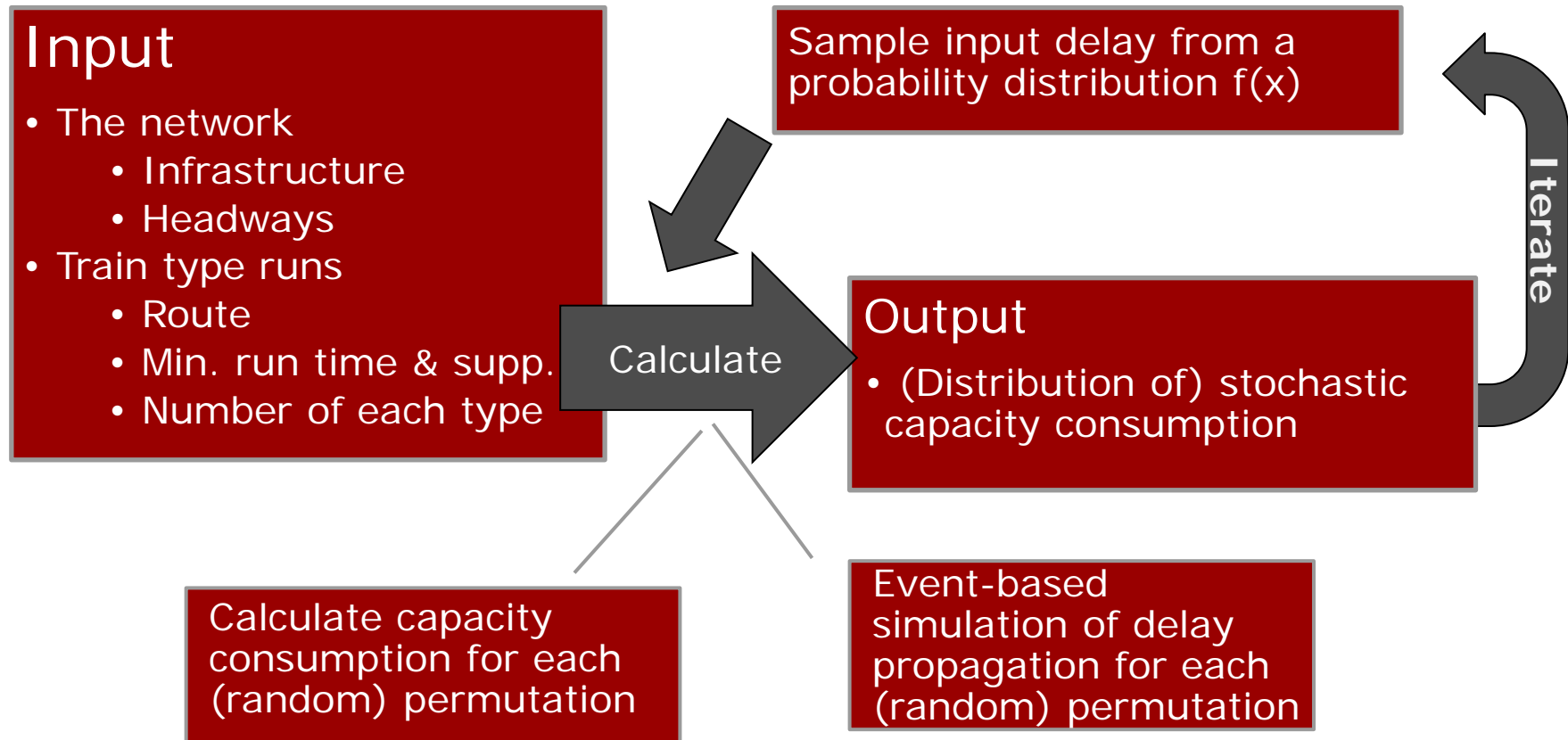


*Permutation with lowest capacity consumption*

*~54% of the permutations are possible to schedule*

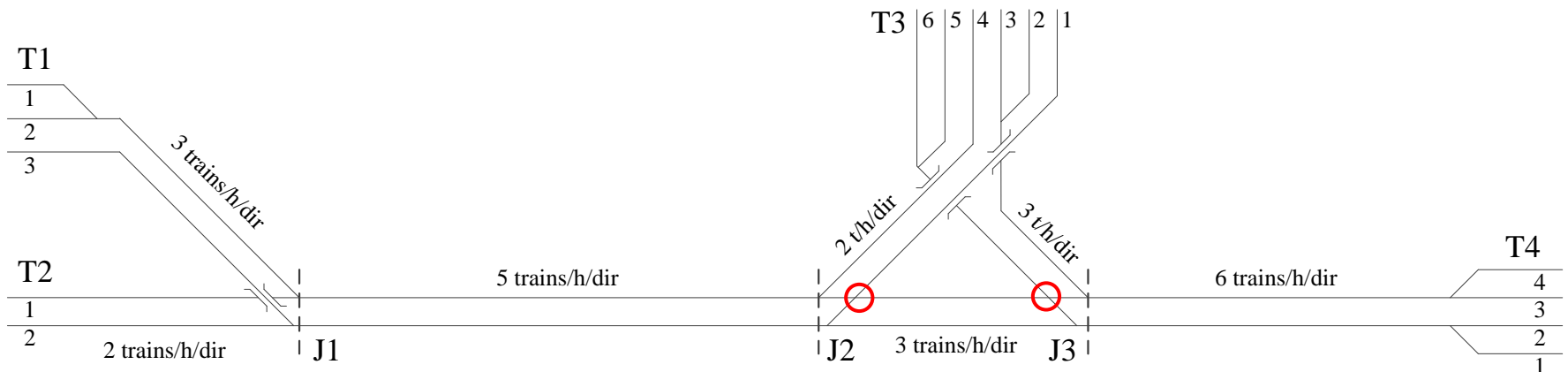
*Permutation with highest capacity consumption*

# Stochastic capacity consumption



# Case

- 16 trains (1 ICE, 2 IC, 2+1 regional & 2 freight per direction)
- Mesoscopic network (feasibility can be ensured by microscopic input data)
- Scenarios:
  - Base: J2 & J3 at-grade junctions
  - J2 upgraded (to out-of-grade)
  - J3 upgraded
  - J2 & J3 upgraded
- Entrance delays at T1-T4 and delays at stops
  - Weibull distributed truncated at 10 minutes (no rescheduling)



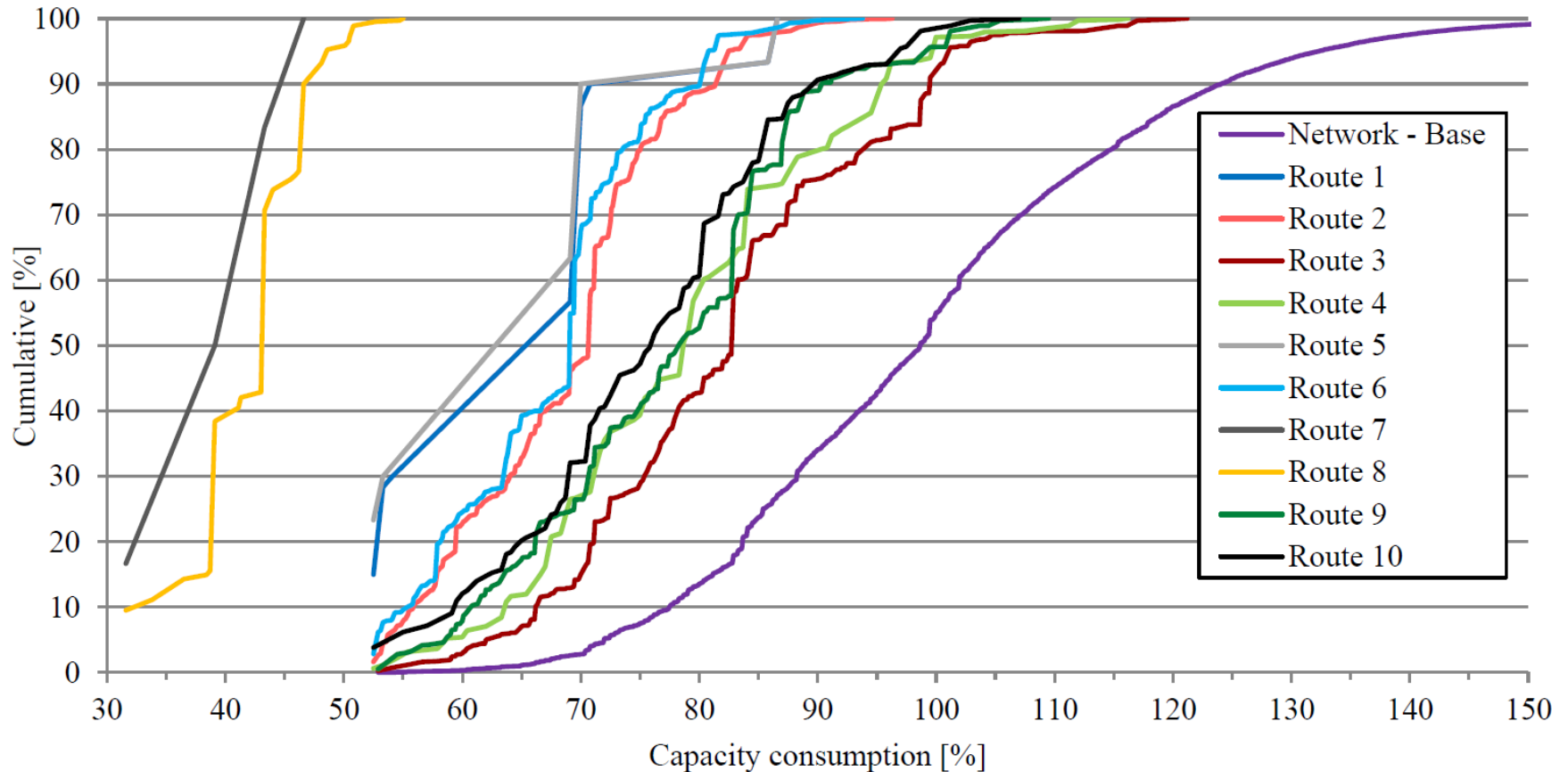
# Computational characteristics and results

- Sample of ~13 mil. permutations
- 60 iterations for stochastic simulation
- 12 seconds computation time for deterministic calculation (whole network)
- ~30 minutes computation time for stochastic calculation

# Deterministic results

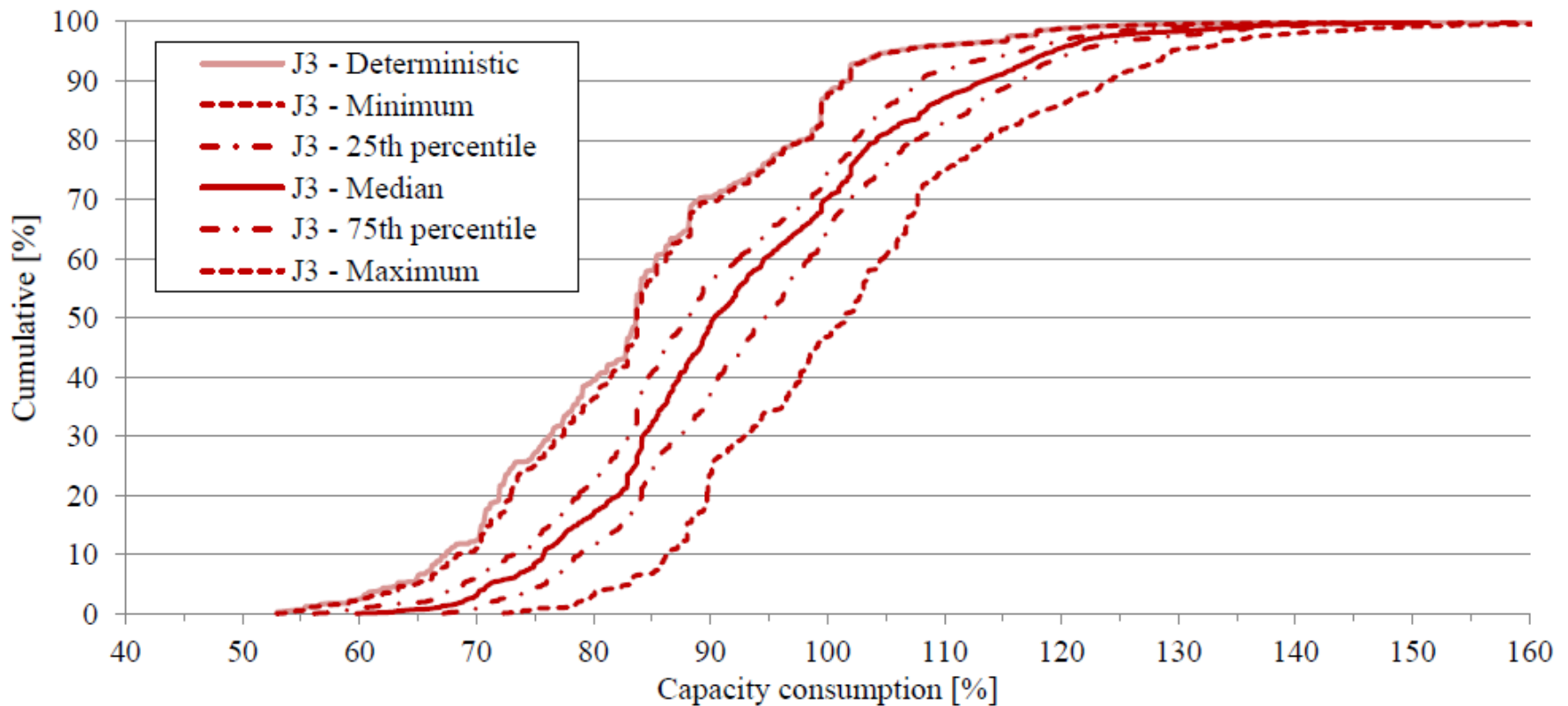
## – impact of assessment area

- Route and network capacity consumption



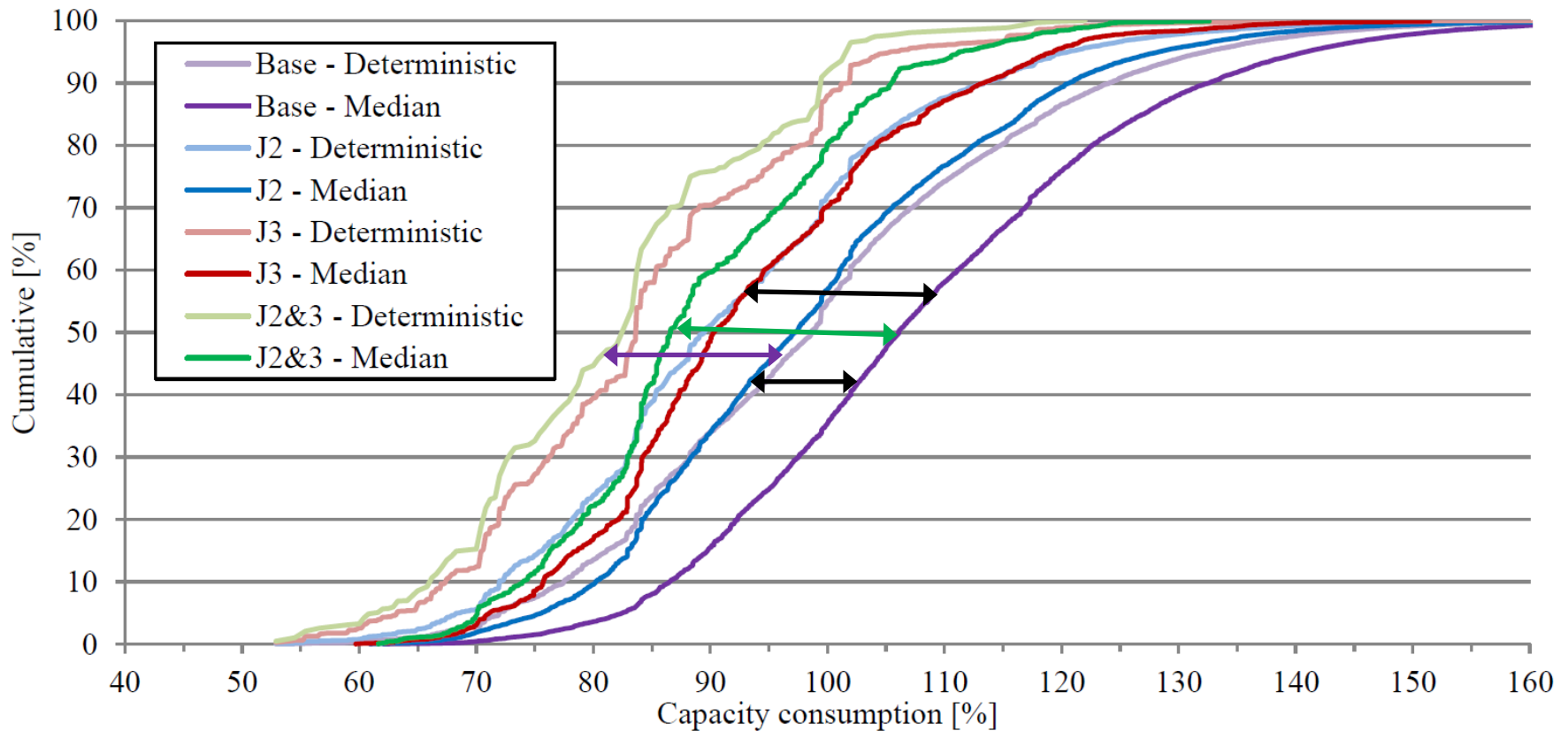
# Stochastic results

- Variance of results over all iterations (60)



# Stochastic results

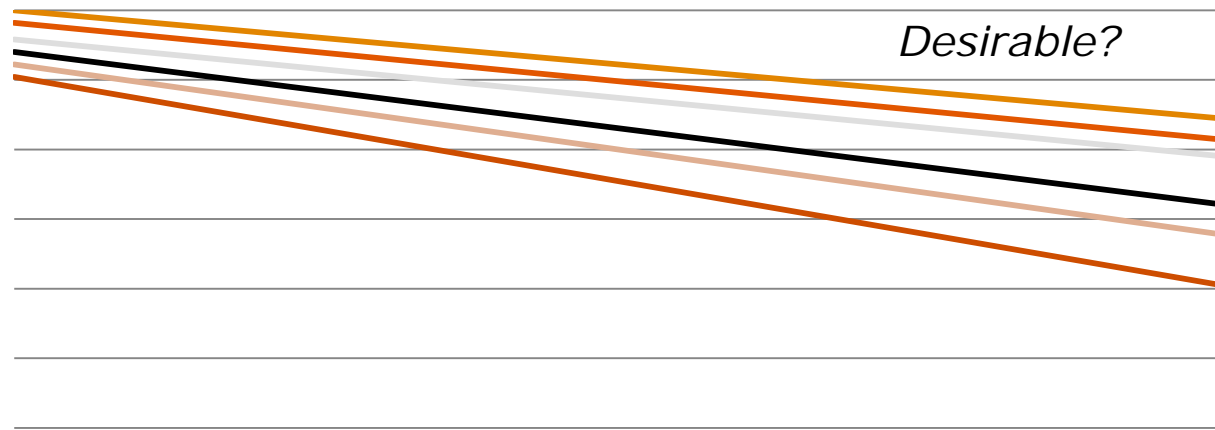
- Four different scenarios:





# Exclusion of certain sequences

Does it make sense to consider all sequences of train runs?



- Exclude “infeasible” train sequences before calculation
  - Using e.g. heterogeneity indicators
  - Exclude certain sequences
    - E.g. all sequence where train A follows train B
  - Use only certain sequences
    - E.g. consider only sequences where train C follows A
    - Can be used to model turn-arounds, couplings and overtakings

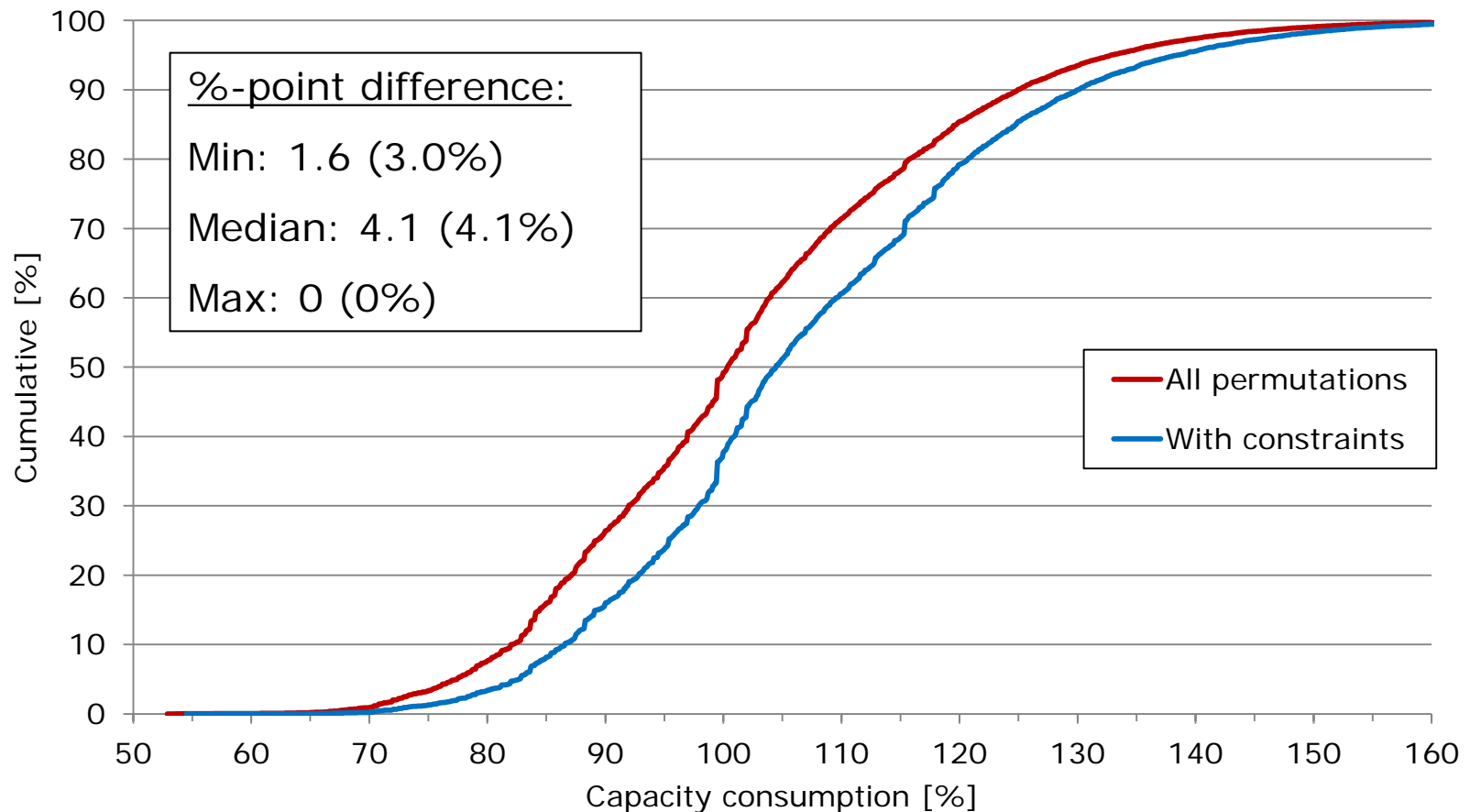
# Constrain sequences

- 2 types:
  1.  $A < X < B$ : train type A cannot flow train type B
  2.  $A < C$ : train type C must follow train type A



# Network capacity consumption results

- Results for constrained vs unconstrained case:



# Conclusions

- Model framework developed for capacity consumption assessment in railway networks
  - No timetable needed
  - Possible to account for delays (stochastic assessment)
- Capacity assessment is very much dependent on the size of the network considered
- Improvement (decrease) in network capacity consumption observed in case when some junctions are upgraded
  - Better improvement for stochastic case than in the deterministic case
- Constrain sequences in case
  - Results are shifted to the right (higher capacity consumption)

# Thank you for your attention!



Lars Wittrup Jensen  
Department of Transport  
Technical University of Denmark  
[lawj@transport.dtu.dk](mailto:lawj@transport.dtu.dk)