## Problem 5: Association Rules - Apriori Algorithm

A database has five transactions. Let min_sup $=60 \%$ and min_confid $=80 \%$

| TID | items_bought |
| :--- | :--- |
| T100 | $\{\mathbf{D}, \mathbf{A}, \mathbf{C}, \mathbf{E}, \mathbf{B}\}$ |
| T200 | $\{\mathbf{K}, \mathbf{A}, \mathbf{G}, \mathbf{D}, \mathbf{B}\}$ |
| T300 | $\{\mathbf{B}, \mathbf{A}, \mathbf{D}\}$ |
| T400 | $\{\mathbf{D}, \mathbf{F}, \mathbf{B}\}$ |
| T500 | $\{\mathbf{C}, \mathbf{A}, \mathbf{B}, \mathbf{E}, \mathbf{K}\}$ |

(a) find all frequent itemsets using Apriori algorithm (assume minimum support count is $\mathbf{3}$ )
(b) list all of the strong association rules (with support, $\boldsymbol{s}$, and confidence, $\boldsymbol{c}$ ) matching the following metarule, where $\boldsymbol{X}$ is a variable representing customers, and item $_{i}$ are variables representing items (e.g., "A", "B", etc.).

$$
\begin{aligned}
& \forall x \in \operatorname{transactio} n, \operatorname{buys}\left(X, \text { item }_{1}\right) \Rightarrow \operatorname{buys}\left(X, \text { item }_{2}\right) \wedge \operatorname{buys}\left(X, \text { item }_{3}\right)[s, c] \\
& \forall x \in \operatorname{transactio} n, \operatorname{buys}\left(X, \text { item }_{1}\right) \wedge \operatorname{buys}\left(X, \text { item }_{2}\right) \Rightarrow \operatorname{buys}\left(X, \text { item }_{3}\right)[s, c]
\end{aligned}
$$

