32. Recursion

Java

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Introduction

Introduction

- Recursive methods
 - A method that invokes itself directly or indirectly.
- Recursion
 - is a useful programming technique
 - It enables you to develop a natural, straightforward, simple solution to a problem that would otherwise be difficult to solve.
- Many mathematical functions are defined using recursion.



 Consider the factorial of a positive integer n, written n! (and pronounced "n factorial"), which is the product

n x (n - 1) x (n - 2) x ... x 1

- with 1! equal to 1 and 0! defined to be 1.
- For example, 5! is the product 5x4x3x2x1, which is equal to 120.



 The factorial of integer n (where n >= 0) can be calculated iteratively (non-recursively) using a for statement as follows:

factorial = 1;

for (int counter = n; counter >= 1; counter--)

factorial = factorial * counter;

- The program:
 - <u>ComputeFactorialIteratively.java</u>

Example: Factorials

- The factorial of a number n can be recursively calculated.
- Let factorial(n) be the method for computing n!.
- If you call the method with n = 0, it immediately returns the result.
- The method knows how to solve the simplest case, which is referred to as the base case or the stopping condition.
- If you call the method with n > 0, it reduces the problem into a subproblem for computing the factorial of n - 1.



- The subproblem is essentially the same as the original problem, but is simpler or smaller than the original.
- Because the subproblem has the same property as the original, you can call the method with a different argument, which is referred to as a recursive call.



 The recursive algorithm for computing factorial(n) can be simply described as follows: if (n == 0)

```
return 1;
```

else

```
return n * factorial(n - 1);
```

- The program:
 - <u>ComputeFactorialRecursively.java</u>



- For a recursive method to terminate, the problem must eventually be reduced to a stopping case.
- When it reaches a stopping case, the method returns a result to its caller.
- The caller then performs a computation and returns the result to its own caller.
- This process continues until the result is passed back to the original caller.

Example: Factorials - Invoking factorial(4)

Factorial(4) = 4 * factorial(3)= 4 * (3 * factorial(2))= 4 * (3 * (2 * factorial(1)))= 4 * (3 * (2 * (1 * factorial(0)))) = 4 * (3 * (2 * (1 * 1))))= 4 * (3 * (2 * 1))= 4 * (3 * 2) = 4 * 6= 24

Example: Factorials - Invoking factorial(4)



Example: Factorials – Memory Space





Recursion Caution • Infinite recursion can occur if recursion does not reduce the problem in a manner that allows it to eventually converge into the base case. • For example, if you mistakenly write the factorial method as follows: public static long factorial(int n) return n * factorial(n - 1);

• The method runs infinitely and causes a StackOverflowError.

Example: Fibonacci Numbers

Example: Fibonacci Numbers

- Consider the well-known Fibonacci series problem, as follows:
 The series: 0 1 1 2 3 5 8 13 21 34 55 89 ...
 indices: 0 1 2 3 4 5 6 7 8 9 10 11
- The Fibonacci series begins with 0 and 1, and each subsequent number is the sum of the preceding two numbers in the series.

Example: Fibonacci Numbers

- The recursive algorithm for computing fib(index) can be simply described as follows:
- if (index == 0)
 - return 0;
- else if (index == 1)

return 1;

else

return fib(index - 1) + fib(index - 2);

• Example:

fib(3) = fib(2) + fib(1) = (fib(1) + fib(0)) + fib(1) = (1 + 0) + fib(1) = 1 + fib(1) = 1 + 1 = 2

Example: Fibonacci Numbers

- The program:
 - <u>ComputeFibonacciRecursively.java</u>



Example: Fibonacci Numbers

- The recursive implementation of the fib method is very simple and straightforward, but not efficient.
- The recursive fib method is a good example to demonstrate how to write recursive methods, though it is not practical.
- See ComputeFibonaccilteratively.java an efficient solution using loops.
 - <u>ComputeFibonaccilteratively.java</u>

- All recursive methods have the following characteristics:
 - The method is implemented using an if-else or a switch statement that leads to different cases.
 - One or more base cases (the simplest case) are used to stop recursion.
 - Every recursive call reduces the original problem, bringing it increasingly closer to a base case until it becomes that case.



- In general, to solve a problem using recursion, you break it into subproblems.
- If a subproblem resembles the original problem, you can apply the same approach to solve the subproblem recursively.
- This subproblem is almost the same as the original problem in nature with a smaller size.

- Both iteration and recursion use a control statement
 - Iteration uses a repetition statement,
 - e.g., for, while or do...while
 - Recursion uses a selection statement
 - e.g., if, if...else or switch



- Both iteration and recursion involve repetition:
 - Iteration explicitly uses a repetition statement,
 - Recursion achieves repetition through repeated method calls.
- Iteration and recursion both involve a termination test
 - Iteration terminates when the loop-continuation condition fails
 - Recursion terminates when a base case is reached



- A recursive approach is normally preferred over an iterative approach when:
 - The recursive approach more naturally mirrors the problem and results in a program that is easier to understand and debug.
 - A recursive approach can often be implemented with fewer lines of code.



- Any problem that can be solved recursively can also be solved iteratively.
- Recursion can be expensive in terms of processor time and memory space
- Avoid using recursion in situations requiring high performance. Recursive calls take time and consume additional memory.

References



The End