## 32. Recursion

Java

Fall 2009<br>Instructor: Dr. Masoud Yaghini

## Outline

- Introduction
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- Recursion vs. Iteration
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## Introduction

## Recursion

## Introduction

- Recursive methods
- A method that invokes itself directly or indirectly.
- Recursion
- is a useful programming technique
- It enables you to develop a natural, straightforward, simple solution to a problem that would otherwise be difficult to solve.
- Many mathematical functions are defined using recursion.


## Example: Factorials

## Example: Factorial

- Consider the factorial of a positive integer n, written n ! (and pronounced "n factorial"), which is the product
$n \times(n-1) \times(n-2) \times \ldots \times 1$
- with 1 ! equal to 1 and 0 ! defined to be 1 .
- For example, 5 ! is the product $5 \times 4 \times 3 \times 2 \times 1$, which is equal to 120.


## Recursion

## Example: Factorial

- The factorial of integer n (where $\mathrm{n}>=0$ ) can be calculated iteratively (non-recursively) using a for statement as follows:
factorial $=1$;
for (int counter $=\mathrm{n}$; counter >=1; counter--)
factorial = factorial * counter;
- The program:
- ComputeFactoriallteratively.java


## Example: Factorials

- The factorial of a number n can be recursively calculated.
- Let factorial(n) be the method for computing n !.
- If you call the method with $\mathrm{n}=0$, it immediately returns the result.
- The method knows how to solve the simplest case, which is referred to as the base case or the stopping condition.
- If you call the method with $n>0$, it reduces the problem into a subproblem for computing the factorial of $\mathrm{n}-1$.


## Example: Factorials

- The subproblem is essentially the same as the original problem, but is simpler or smaller than the original.
- Because the subproblem has the same property as the original, you can call the method with a different argument, which is referred to as a recursive call.


## Example: Factorials

- The recursive algorithm for computing factorial(n) can be simply described as follows: if ( $\mathrm{n}==0$ )
return 1;
else
return n * factorial(n-1);
- The program:
- ComputeFactorialRecursively.java


## Example: Factorials

- For a recursive method to terminate, the problem must eventually be reduced to a stopping case.
- When it reaches a stopping case, the method returns a result to its caller.
- The caller then performs a computation and returns the result to its own caller.
- This process continues until the result is passed back to the original caller.


## Example: Factorials - Invoking factorial(4)

Factorial(4) $=4$ * factorial(3)

$$
\begin{aligned}
& =4 *(3 * \text { factorial }(2)) \\
& =4^{*}(3 *(2 * \text { factorial(1))) } \\
& =4^{*}\left(3^{*}(2 *(1 * \text { factorial(0)))) }\right. \\
& \left.=4^{*}\left(3^{*}\left(2 *\left(1^{*} 1\right)\right)\right)\right) \\
& =4^{*}\left(3^{*}(2 * 1)\right) \\
& =4^{*}(3 * 2) \\
& =4 * 6 \\
& =24
\end{aligned}
$$

## Example: Factorials - Invoking factorial(4)



## Recursion

## Example: Factorials - Memory Space



## Caution

- It is simpler and more efficient to implement the factorial method using a loop.
- However, the recursive factorial method is a good example to demonstrate the concept of recursion.


## Caution

- Infinite recursion can occur if recursion does not reduce the problem in a manner that allows it to eventually converge into the base case.
- For example, if you mistakenly write the factorial method as follows:
public static long factorial(int n)
\{
return n * factorial(n-1);
- The method runs infinitely and causes a StackOverflowError.


## Example: Fibonacci Numbers

## Example: Fibonacci Numbers

- Consider the well-known Fibonacci series problem, as follows:
The series: 01123581321345589 ... indices: $\quad 01234567891011$
- The Fibonacci series begins with 0 and 1, and each subsequent number is the sum of the preceding two numbers in the series.


## Recursion

## Example: Fibonacci Numbers

- The recursive algorithm for computing fib(index) can be simply described as follows:

```
if (index == 0)
    return 0;
else if (index == 1)
    return 1;
else
    return fib(index - 1) + fib(index - 2);
```

- Example:

$$
\begin{aligned}
\mathrm{fib}(3) \quad & =\mathrm{fib}(2)+\mathrm{fib}(1) \\
& =(\mathrm{fib}(1)+\mathrm{fib}(0))+\mathrm{fib}(1) \\
& =(1+0)+\mathrm{fib}(1) \\
& =1+\mathrm{fib}(1) \\
& =1+1 \\
& =2
\end{aligned}
$$

## Example: Fibonacci Numbers

- The program:
- ComputeFibonacciRecursively.java



## Example: Fibonacci Numbers

- The recursive implementation of the fib method is very simple and straightforward, but not efficient.
- The recursive fib method is a good example to demonstrate how to write recursive methods, though it is not practical.
- See ComputeFibonaccilteratively.java an efficient solution using loops.
- ComputeFibonaccilteratively.java


## Recursion vs. Iteration

## Recursion vs. Iteration

- All recursive methods have the following characteristics:
- The method is implemented using an if-else or a switch statement that leads to different cases.
- One or more base cases (the simplest case) are used to stop recursion.
- Every recursive call reduces the original problem, bringing it increasingly closer to a base case until it becomes that case.


## Recursion vs. Iteration

- In general, to solve a problem using recursion, you break it into subproblems.
- If a subproblem resembles the original problem, you can apply the same approach to solve the subproblem recursively.
- This subproblem is almost the same as the original problem in nature with a smaller size.


## Recursion

## Recursion vs. Iteration

- Both iteration and recursion use a control statement
- Iteration uses a repetition statement,
- e.g., for, while or do...while
- Recursion uses a selection statement
- e.g., if, if...else or switch


## Recursion vs. Iteration

- Both iteration and recursion involve repetition:
- Iteration explicitly uses a repetition statement,
- Recursion achieves repetition through repeated method calls.
- Iteration and recursion both involve a termination test
- Iteration terminates when the loop-continuation condition fails
- Recursion terminates when a base case is reached


## Recursion vs. Iteration

- A recursive approach is normally preferred over an iterative approach when:
- The recursive approach more naturally mirrors the problem and results in a program that is easier to understand and debug.
- A recursive approach can often be implemented with fewer lines of code.


## Recursion vs. Iteration

- Any problem that can be solved recursively can also be solved iteratively.
- Recursion can be expensive in terms of processor time and memory space
- Avoid using recursion in situations requiring high performance. Recursive calls take time and consume additional memory.


## References

## Recursion

## References

- Y. Daniel Liang, Introduction to Java Programming, Sixth Edition, Pearson Education, 2007. (Chapter 19)
- H. M. Deitel and P. J. Deitel, Java ${ }^{\text {TM }}$ How to Program, Sixth Edition, Prentice Hall, 2005. (Chapter 15)


## The End

