



LINGO 8.0 Software

مدرس: دكتور مسعود يقيني

Introduction to LINGO 8.0

- LINGO is a software tool designed to efficiently build and solve linear, nonlinear, and integer optimization models



Creating a LINGO Model

- An Optimization model consists of 3 parts
 - Objective Function
 - A single formula that describes exactly what the model should optimize
 - Variables
 - Quantities that can be changed to produce the optimal value of the objective function
 - Constraints
 - formulas that define the limits on the values of the variables



A Sample Model

! A cookie store can produce drop cookies and decorated cookies, which sell for \$1 and \$1.50 apiece, respectively. The two bakers each work 8 hours per day and can produce up to 400 drop cookies and 200 decorated cookies. It takes 1 minute to produce each drop cookie and 3 minutes to produce each decorated cookie. What combination of cookies produced will maximize the baker's profit? ;

$$\text{MAX} = 1 * \text{Drop} + 1.5 * \text{Deco};$$

$$\text{Drop} \leq 400;$$

$$\text{Deco} \leq 200;$$

$$1/60 * \text{Drop} + 3/60 * \text{Deco} \leq 16;$$



Things to notice

- Comments in the model are initiated with an exclamation point (!) and appear in green text
- LINGO specified operators and functions appear in blue text
- All other text is shown in black
- Each LINGO statement must end in a semi-colon (;)
- Variable names are not case-sensitive and must begin with a letter (A-Z)



Solving a LINGO Model

- Once the model has been entered into the Model Window, it can be solved by:
 - clicking the *Solve* button
 - Selecting Solve from the LINGO menu
 - Using the ctrl+s keyboard shortcut
- Errors (if any) will be reported



LINGO Solver Status Window

- If no errors are found, the LINGO Solver Status window appears



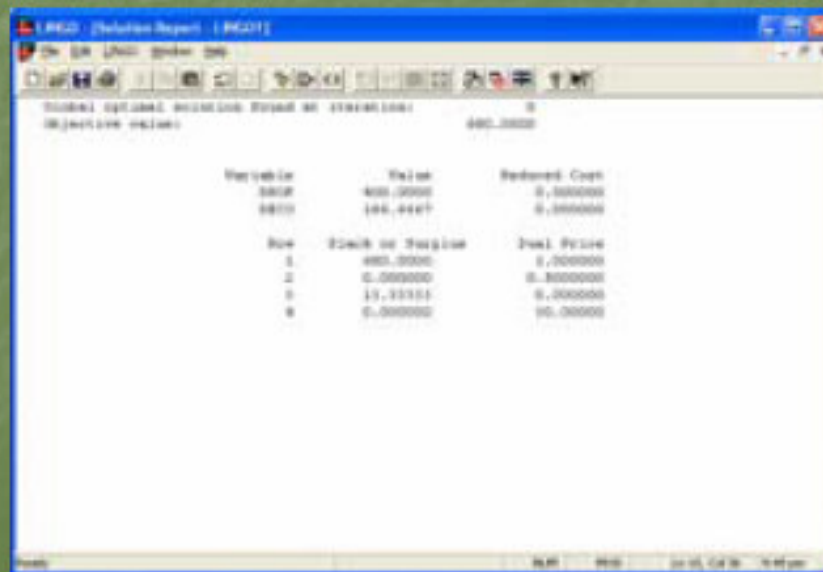
LINGO Solver Status [LINGO1] ✖

Solver Status		Variables	
Model Class:	IP	Total:	2
State:	Global Optimum	Nonlinear:	0
Objective:	680	Integers:	0
Infeasibility:	0	Constraints	
Iterations:	0	Total:	4
Extended Solver Status		Nonlinear:	0
Solver Type	. . .	Nonzeros	
Best Obj:	. . .	Total:	6
Obj Bound:	. . .	Nonlinear:	0
Steps:	. . .	Generator Memory Used (K)	
Active:	. . .	5	
Update Interval: <input type="text" value="2"/>		Elapsed Runtime (hh:mm:ss)	
<input type="button" value="Interrupt Solver"/>		00 : 00 : 00	
		<input type="button" value="Close"/>	



LINGO Solution Report Window

- Close the Solver Status window to see the Solution Report window



The screenshot shows the LINGO Solution Report window. At the top, it displays the title 'LINGO [Solution Report - LINGO1]' and the status 'The LP (LINGO) solver has' followed by a toolbar. Below the toolbar, it states 'TOTAL OPTIMAL INCLUDING FIXED BY CONSTRAINTS' with a value of 0 and 'OBJECTIVE VALUE' with a value of 480.0000. The main content is a table with three columns: Variable, Value, and Reduced Cost. The first two rows show variables with values 480.0000 and 144.4447, both with a reduced cost of 0.000000. Below this is a section for rows, with columns 'Row', 'Status or Range', and 'Dual Price'. The rows are numbered 1 through 4, with dual prices of 1.000000, 0.000000, 0.000000, and 10.000000 respectively.

Variable	Value	Reduced Cost
OBJ	480.0000	0.000000
OBJ	144.4447	0.000000
Row	Status or Range	Dual Price
1	480.0000	1.000000
2	0.000000	0.000000
3	15.55555	0.000000
4	0.000000	10.00000



LINGO Solution Report Window

- Slack or Surplus
 - Zero if a constraint is completely satisfied as an equality
 - Positive shows how many more units of the variable could be added to the optimal solution before the constraint becomes an equality
 - Constraint has been violated if negative



LINGO Solution Report Window

- Reduced Cost
 - How much the objective function would degrade if one unit of a variable (not included in the current solution) were to be included
- Dual Price
 - How much the objective function would improve if the constraining value is increased by one unit



Using Sets in LINGO

- LINGO allows you to group many instances of the same variable into sets
 - Example: If a model involved 27 delivery trucks, then these 27 trucks could be described more simply as a single set
- Sets may also include attributes for each member, such as the hauling capacity for each delivery truck



Using Sets

- *SETS* section must be defined before any of the set members are used in the model's constraints
- Primitive set example:

```
SETS :
```

```
    Trucks/TR1..TR27/ :Capacity;
```

```
ENDSETS
```



Set Looping Statement Examples

```
@FOR (Trucks (T) : Capacity (T) <= 3000) ;
```

- This @FOR statement sets the hauling capacity for all 27 delivery trucks in the Trucks set to at most 3000 pounds

```
TOTAL_HAUL=@SUM (Trucks (J) : Capacity (J)) ;
```

- This @SUM statement calculates the total hauling capacity from the individual trucks



LINGO Data Example

SETS:

```
    SET1 /A, B, C/: X, Y;
```

ENDSETS

DATA:

```
    X = 1, 2, 3;
```

```
    Y = 4, 5, 6;
```

ENDDATA



Variable Types in LINGO

- All variables in a LINGO model are considered to be non-negative and continuous unless otherwise specified
- LINGO's four variable domain functions can be used to override the default domain for given variables



Variable Types in LINGO (cont.)

- @GIN – any positive integer value
- @BIN – a binary value (ie, 0 or 1)
- @FREE – any positive or negative real value
- @BND – any value within the specified bounds



Mathematical Functions

- @ABS(X) – returns the absolute value of X
- @SIGN(X) – returns -1 if X is negative and +1 if X is positive
- @EXP(X) – calculates e^X
- @LOG(X) – calculates the natural log of X
- @SIN(X) – returns the sine of X , where X is the angle in radians
- @COS(X) – returns the cosine of X
- @TAN(X) – returns the tangent of X



An Example



Example

- Bisco's new sugar-free, fat-free chocolate squares are so popular that the company cannot keep up with demand. Regional demands shown in the following table total 2000 cases per week, but Bisco can produce only 60% (1200 cases) of that number.

	NE	SE	MW	W
Demand	620	490	510	380
Profit	1.6	1.4	1.9	1.2

- The table also shows the different profit levels per case experienced in the regions due to competition and consumer tastes. Bisco wants to find a maximum profit plan that fulfils between 50% and 70% of each region's demand.

Problem Formulation



$$\max \sum_{i=1}^4 p_i x_i$$

$$\sum_{i=1}^4 x_i \leq 1200$$

$$l_i \leq x_i \leq u_i, i = 1, 2, 3, 4$$

Problem Formulation (con.)



$$\max 1.60 x_1 + 1.40 x_2 + 1.90 x_3 + 1.20 x_4$$

$$x_1 + x_2 + x_3 + x_4 \leq 1200$$

$$x_1 \geq 310$$

$$x_1 \leq 434$$

$$x_2 \geq 245$$

$$x_2 \leq 343$$

$$x_3 \geq 255$$

$$x_3 \leq 357$$

$$x_4 \geq 190$$

$$x_4 \leq 266$$



LINGO Solution - 1

```
max= 1.60 *x1 + 1.40* x2 + 1.90 *x3 + 1.20 *x4;  
x1 + x2 + x3 + x4 <=1200;  
x1 >= 310;  
x1 <= 434;  
x2 >= 245;  
x2 <= 343;  
x3 >= 255;  
x3 <= 357;  
x4 >= 190;  
x4 <= 266;
```

LINGO Solution 1 (con.)



Global optimal solution found at iteration: 4
Objective value: 1902.100

Variable	Value	Reduced Cost
X1	408.0000	0.000000
X2	245.0000	0.000000
X3	357.0000	0.000000
X4	190.0000	0.000000
X5	0.000000	0.000000

Row	Slack or Surplus	Dual Price
1	1902.100	1.000000
2	0.000000	1.600000
3	98.00000	0.000000
4	26.00000	0.000000
5	0.000000	-0.2000000
6	98.00000	0.000000
7	102.0000	0.000000
8	0.000000	0.3000000
9	0.000000	-0.4000000
10	266.0000	0.000000



LINGO Solution 2 (con.)

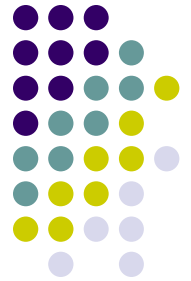
- **Defining sets**

SETS:

```
REGIONS / NE SE MW W/: LBOUND,  
UBOUND, PROFIT, CASES;
```

ENDSETS

- Each of the elements in the set has four attributes: LBOUND, UBOUND, PROFIT, and CASES
- The last one being the decision variable and the others being constants.



LINGO Solution 2 (con.)

- Enter the data

DATA:

LBOUND = 310 245 255 190;

UBOUND = 434 343 357 266;

PROFIT = 1.6 1.4 1.9 1.2;

ENDDATA



LINGO Solution 2 (con.)

- **Objective function**

```
MAX = @SUM(REGIONS(I):  
PROFIT(I)*CASES(I));
```



LINGO Solution 2 (con.)

- **Capacity constraint**

```
@SUM(REGIONS(I): CASES(I)) <=1200;
```

- **Minimum/maximum cases**

```
@FOR(REGIONS(I):  
CASES(I) <= UBOUND(I);  
CASES(I) >= LBOUND(I));
```

LINGO Solution 2 (con.)



Global optimal solution found at iteration: 6
 Objective value: 1902.100

Variable	Value	Reduced Cost
LBOUND(NE)	310.0000	0.000000
LBOUND(SE)	245.0000	0.000000
LBOUND(MW)	255.0000	0.000000
LBOUND(W)	190.0000	0.000000
UBOUND(NE)	434.0000	0.000000
UBOUND(SE)	343.0000	0.000000
UBOUND(MW)	357.0000	0.000000
UBOUND(W)	266.0000	0.000000
PROFIT(NE)	1.600000	0.000000
PROFIT(SE)	1.400000	0.000000
PROFIT(MW)	1.900000	0.000000
PROFIT(W)	1.200000	0.000000
CASES(NE)	408.0000	0.000000
CASES(SE)	245.0000	0.000000
CASES(MW)	357.0000	0.000000
CASES(W)	190.0000	0.000000

Row	Slack or Surplus	Dual Price
1	1902.100	1.000000
2	0.000000	1.600000
3	26.00000	0.000000
4	98.00000	0.000000
5	98.00000	0.000000
6	0.000000	-0.2000000
7	0.000000	0.3000000
8	102.0000	0.000000
9	76.00000	0.000000
10	0.000000	-0.4000000



درس برنامه ریزی حرکت قطارها

پیوست ۱:

نرم افزار Lingo

مدرس: دکتر مسعود یقینی