

# A Combined Blocking, Makeup and Scheduling Model

مدرس: دکتر مسعود یقینی

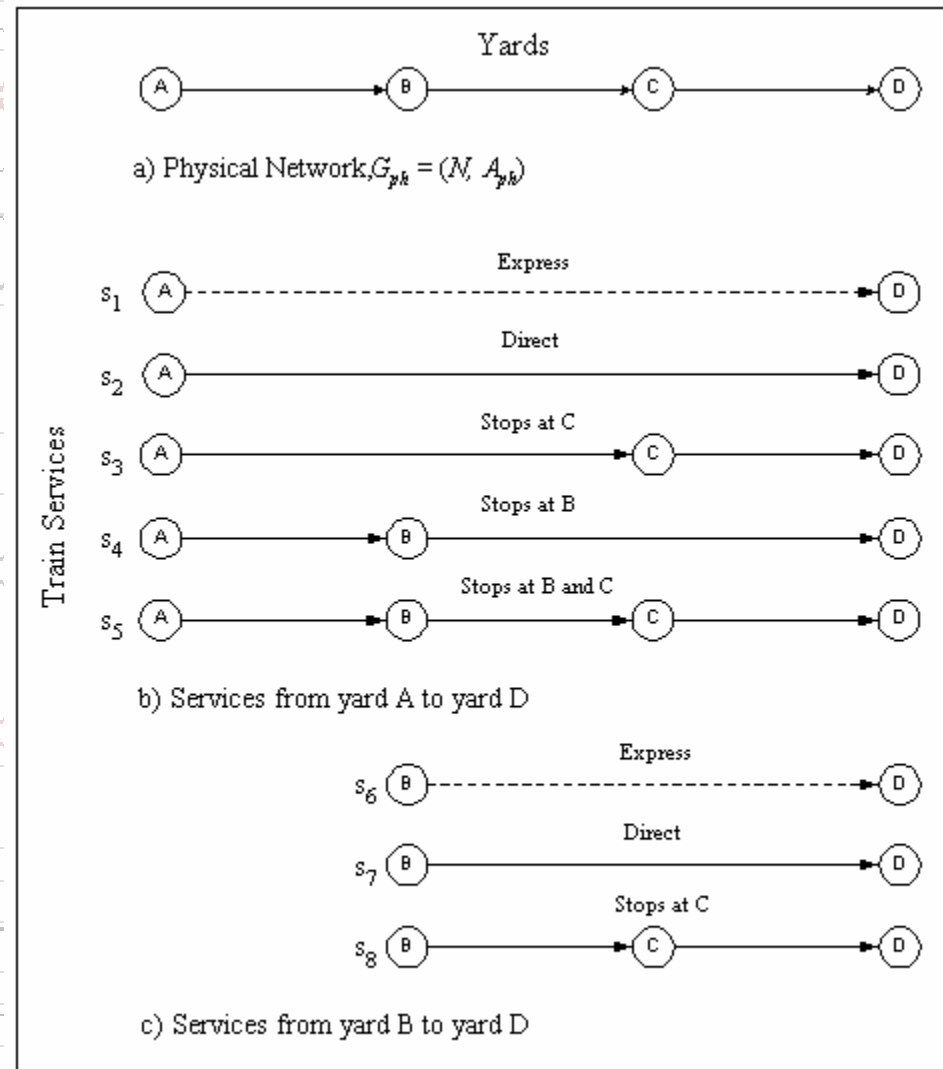
# Contents

- **The objective of this optimization model is to determine train routing, makeup, and scheduling simultaneously. This compound model is constructed to answer the following important railroad operating questions:**
  - (1) On what routes should trains run, at what speed priority and at what frequencies?**
  - (2) Which pairs of terminals are to be provided with direct train connections?**
  - (3) For each freight class, what train sequence should be used and what operations should be performed on the cars at each intermediary stop?**
  - (4) How are cars physically grouped within trains?**
  - (5) What time do trains run?**

# Contents

- The Service Network Design
  - **The Static Service Network Design**
  - **The Dynamic Service Network Design**

# The Static Service Network Design

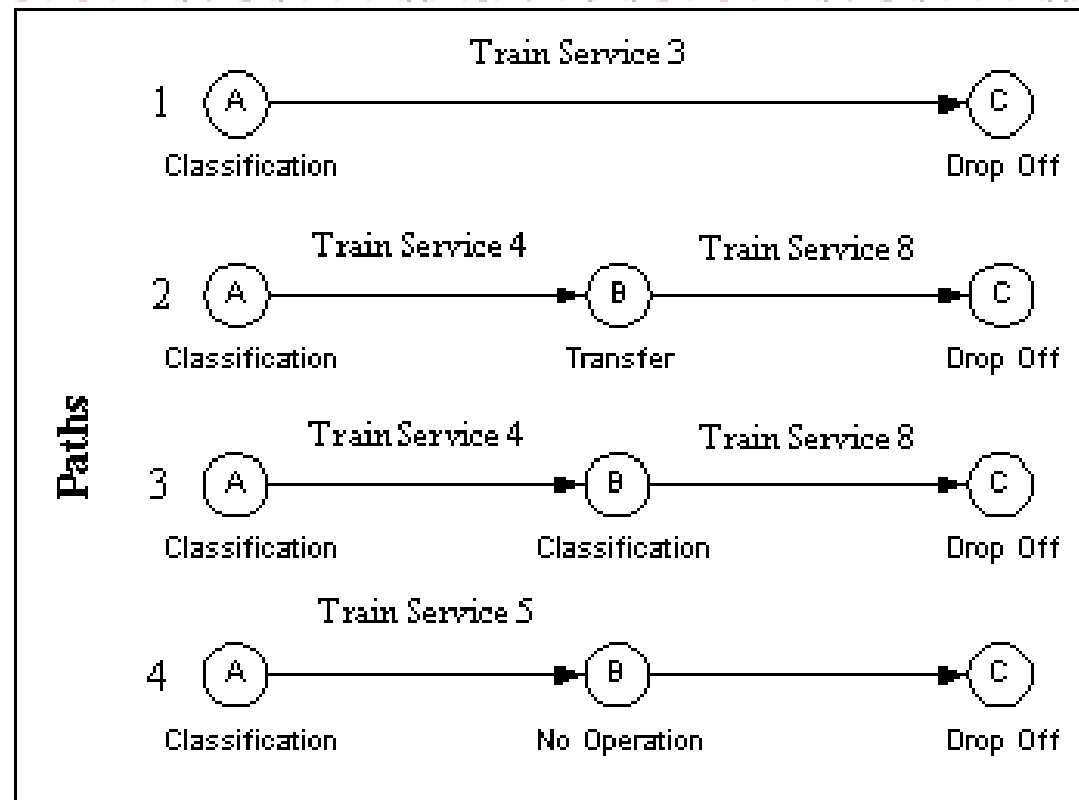


# The Static Service Network Design

On static service network, a service is characterized by:

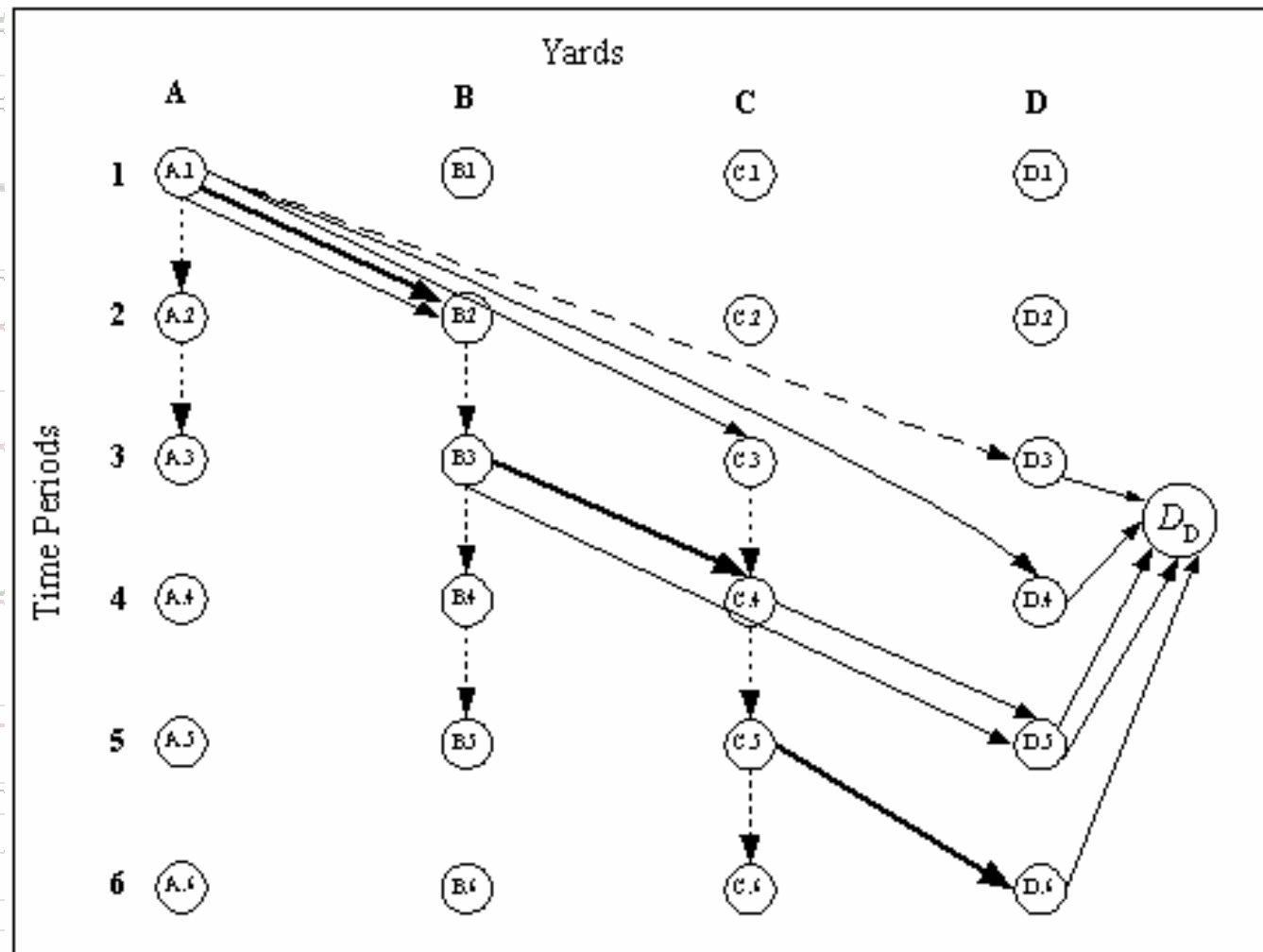
- An origin,
- A destination,
- A set of service links from origin to destination,
- A set of intermediate stops,
- A specification of the type of service in terms of speed and priority.

# The Static Service Network Design



Four Paths for the Traffic from Yard A to Yard C

# The Dynamic Service Network Design



The Dynamic Service Network Design

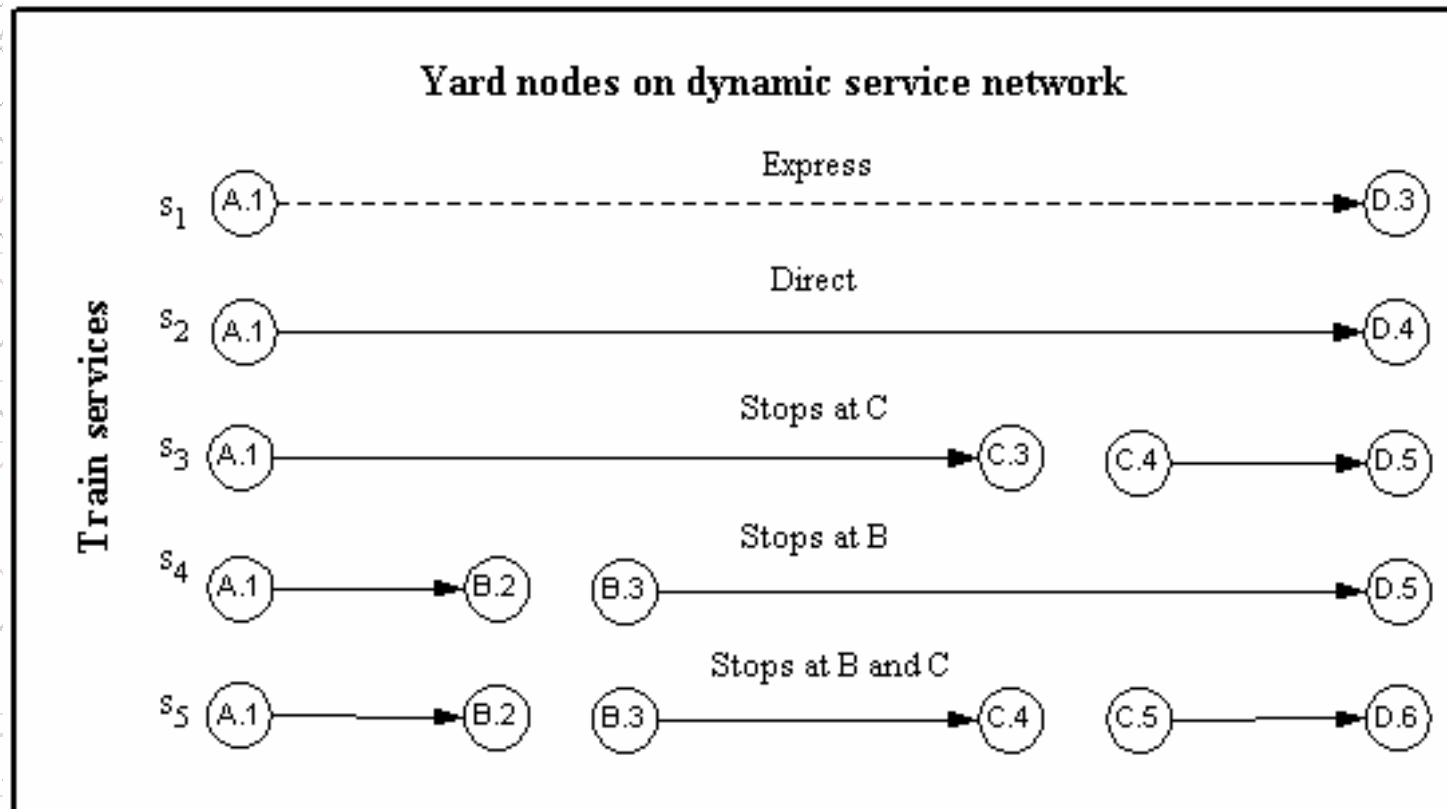
# The Dynamic Service Network Design

In the dynamic network each service has all the specification of a service in static service network plus:

- A departure time from its origin,
- Arrival time and departure times in intermediate stops, and
- Arrival time at the destination.



# The Dynamic Service Network Design



Service Legs of Some Train Services from Yard A to Yard D  
On Dynamic Network Design

# Characteristics of Proposed Models

- **Formulation Structure:** Deterministic Dynamic Service Network Design (similar to fixed-charge, Capacitated, Multicommodity Network Design (*CMND*) formulation)
- **Planning horizon:** Operational and Tactical
- **Program horizon:** Day
- **Time period:** Hour
- **Train running time:** Fixed
- **Switching operation time:** Fixed

# Characteristics of Proposed Models

- Objective: Minimizing Operating and Time Costs
- Costs:
  - **Fixed cost of a train**, (mainly crew costs)
  - **Intermediate yard costs**, (for switching operation)
  - **Car-time cost**, (Time Cost)
  - **Cost of additional horsepower per car**, (for faster trains)
  - **Penalty costs**, (to penalize delivery before and/or after a specified due date)

# Formulation 1: Arc-node Based Model

## Notation

### *Indices:*

$i$  : index for nodes,  $i \in (I, D)$

$j$  : index for track sections between consecutive yards,  $j \in J$

$k$  : index for demands,  $k \in K$

$l$  : index for links,  $l \in L$

$n$  : index for yards (terminals),  $n \in N$

$s$  : index for train services,  $s \in S$

$t$  : index for time periods,  $t = 0, 1, 2, \dots, T$

# Formulation 1: Arc-node Based Model

## *Sets:*

$I$ : the set of yard nodes

$D$ : the set of super nodes

$N$ : the set of yards (terminals)

$J$ : the set of track sections

$K$ : the set of demands

$L$ : the set of links,  $L = \{ L^s, L^h, L^p \}$

$L^s$ : the set of service links

$L^h$ : the set of inventory links

$L^p$ : the set of penalty (super) links

$L_i^+$ : the set of links incident to node  $i \in (I, D)$

$L_i^-$ : the set of links emanating from node  $i \in (I, D)$

# Formulation 1: Arc-node Based Model

## *Parameters:*

$f_s$  : the fixed cost of running train  $s \in S$

$c_l^k$  : the unit cost of moving demand  $k \in K$  on link  $l \in L$

$u_{sl}$  : the total capacity of train service  $s \in S$  on service link  $l \in \Pi_s$

$b_i^k$  : the net flow of demand  $k \in K$ , at node  $i \in (I, D)$

## *Decision Variables:*

$y_s$  : binary variable, 1 if providing train service  $s \in S$ , 0 otherwise

$x_l^k$  : the flow on link  $l \in L$  of demand  $k \in K$

# Arc-node Based Model

$$\text{minimize } Z = \sum_{s \in S} f_s y_s + \sum_{k \in K} \sum_{l \in L} c_l^k x_l^k \quad (1)$$

subject to

$$\sum_{l \in L_i^+} x_l^k - \sum_{l \in L_i^-} x_l^k = b_i^k \quad \text{for all } i \in (I, D), k \in K \quad (2)$$

$$\sum_{k \in K} x_l^k \leq u_{sl} y_s \quad \text{for all } s \in S, l \in \Pi_s \quad (3)$$

$$y_s \in \Omega \quad \text{for all } s \in S \quad (4)$$

$$y_s \in \{0, 1\} \quad \text{for all } s \in S \quad (5)$$

$$x_l^k \geq 0 \text{ and integer} \quad \text{for all } k \in K, l \in L \quad (6)$$

# Arc-node Based Model

## *Link Capacity Constraints*

No more than a specified number of trains may be on a link over some period time

$$\sum_{s \in S_{jt}^c} y_s \leq \varphi_{jt} \quad \text{for all } j \in J, t$$

## *Yard Capacity Constraints*

limit the number of trains, which can be serviced (break up or make up operations) at each yard for each time period

$$\sum_{s \in S_{nt}^d} y_s \leq \beta_{nt} \quad \text{for all } n \in N, t$$

limit the number of train stocks, which each yard can have

$$\sum_{s \in S_{nt}^e} y_s \leq \theta_{nt} \quad \text{for all } n \in N, t$$



# Arc-node Based Model

$$\text{minimize } Z = \sum_{s \in S} f_s y_s + \sum_{k \in K} \sum_{l \in L} c_l^k x_l^k \quad (1)$$

subject to

$$\sum_{l \in L_i^+} x_l^k - \sum_{l \in L_i^-} x_l^k = b_i^k \quad \text{for all } i \in (I, D), k \in K \quad (2)$$

$$\sum_{k \in K} x_l^k \leq u_{sl} y_s \quad \text{for all } s \in S, l \in \Pi_s \quad (3)$$

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# Formulation 2: Path-based Model

## Notation

### *Parameters*

$w_p^k$ : the unit cost of demand  $k \in K$  on path  $p \in P^k$

$\delta_{sl}^{pk}$ : 1 if link  $l \in \Pi_s$  of service  $s \in S$  is used by path  $p \in P^k$  of demand  $k \in K$ , 0 otherwise

### *Decision Variables*

$h_p^k$ : the flow of demand  $k \in K$ , on path  $p \in P^k$

# Path-based Model

$$\text{minimize } Z = \sum_{s \in S} f_s y_s + \sum_{k \in K} \sum_{p \in P^k} w_p^k h_p^k \quad (1)$$

subject to

$$\sum_{p \in P^k} h_p^k = b^k \quad \text{for all } k \in K \quad (2)$$

$$\sum_{k \in K} \sum_{p \in P^k} h_p^k \delta_{sl}^{pk} \leq u_{sl} y_s \quad \text{for all } s \in S, l \in \Pi_s \quad (3)$$

$$y_s \in \Omega \quad \text{for all } s \in S \quad (4)$$

$$y_s \in \{0, 1\} \quad \text{for all } k \in K \quad (5)$$

$$h_p^k \geq 0 \text{ and integer} \quad \text{for all } k \in K, p \in P^k \quad (6)$$

# Comparisons of Models

- Advantages of path-based formulation:
  - **Route costs can be easily incorporated in path model but not in arc model**
  - **Certain classes of constraints that are difficult, if not impossible, to write for arc model are easily defined in path formulation**
  - **The number of constraints in path model is greatly reduced comparing to the number in arc model**
- Disadvantage of path-based formulation:
  - **The increase in the number of decision variables**

# Algorithmic Ideas (continue)

Formulation when all the design trains  $y_s$  ( $s \in S$ ) are open.  
(Similar to a capacitated multicommodity minimum cost network flow (MCNF) problem in path flow variables)

$$\text{minimize } Z = \sum_{k \in K} \sum_{p \in P^k} w_p^k h_p^k$$

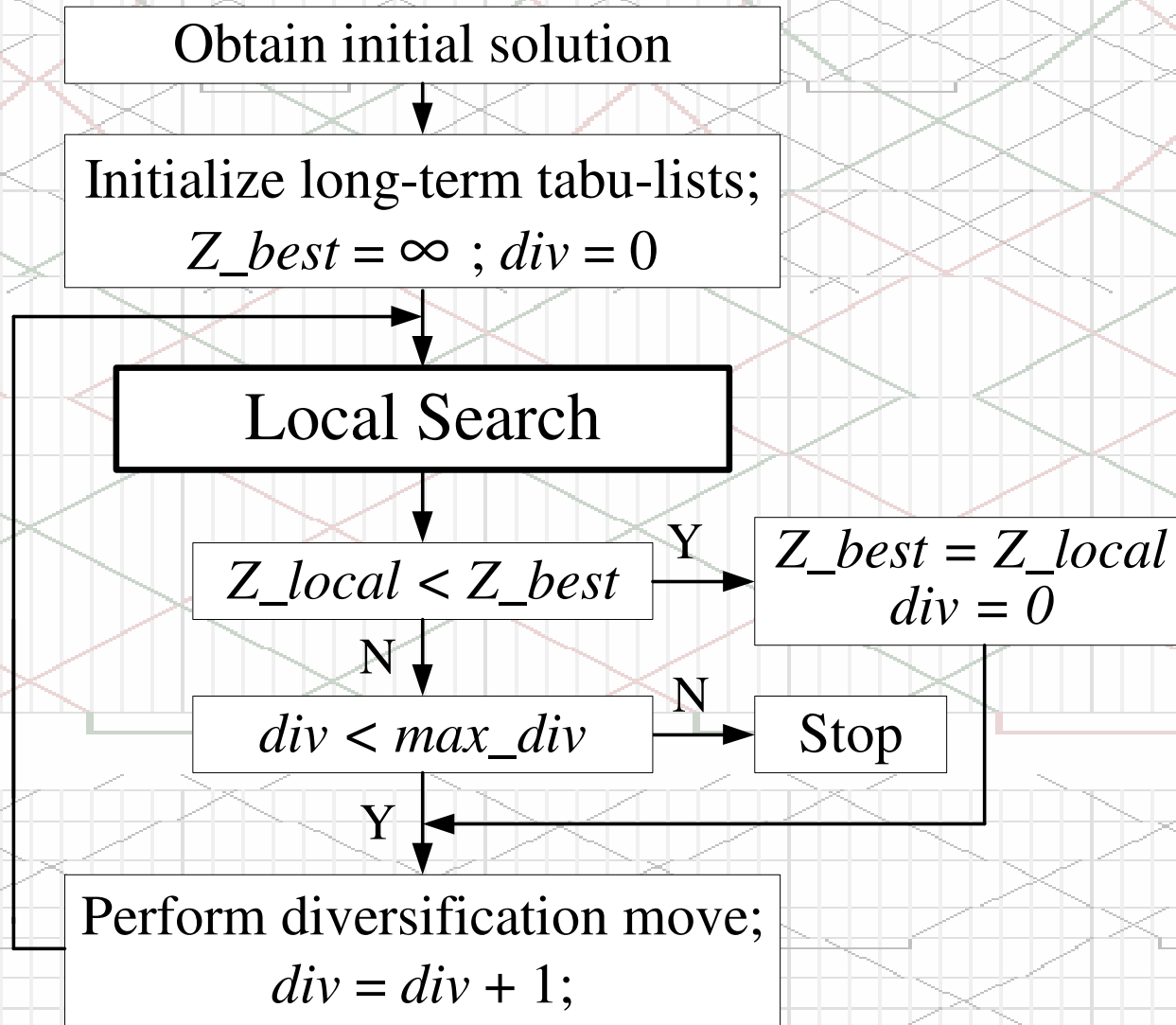
subject to

$$\sum_{p \in P^k} h_p^k = b^k \quad \text{for all } k \in K$$

$$\sum_{k \in K} \sum_{p \in P^k} h_p^k \delta_{sl}^{pk} \leq u_{sl} \quad \text{for all } s \in S, l \in \Pi_s$$

$$h_p^k \geq 0 \text{ and integer for all } k \in K, p \in P^k$$

# Proposed Tabu Search Method



# Proposed Tabu Search Method

- ***Long-term frequency memory***: how many iterations a train has been in the basis
- ***Long-term tabu list***: the trains and paths which are closed each diversification move

# Proposed Tabu Search Method

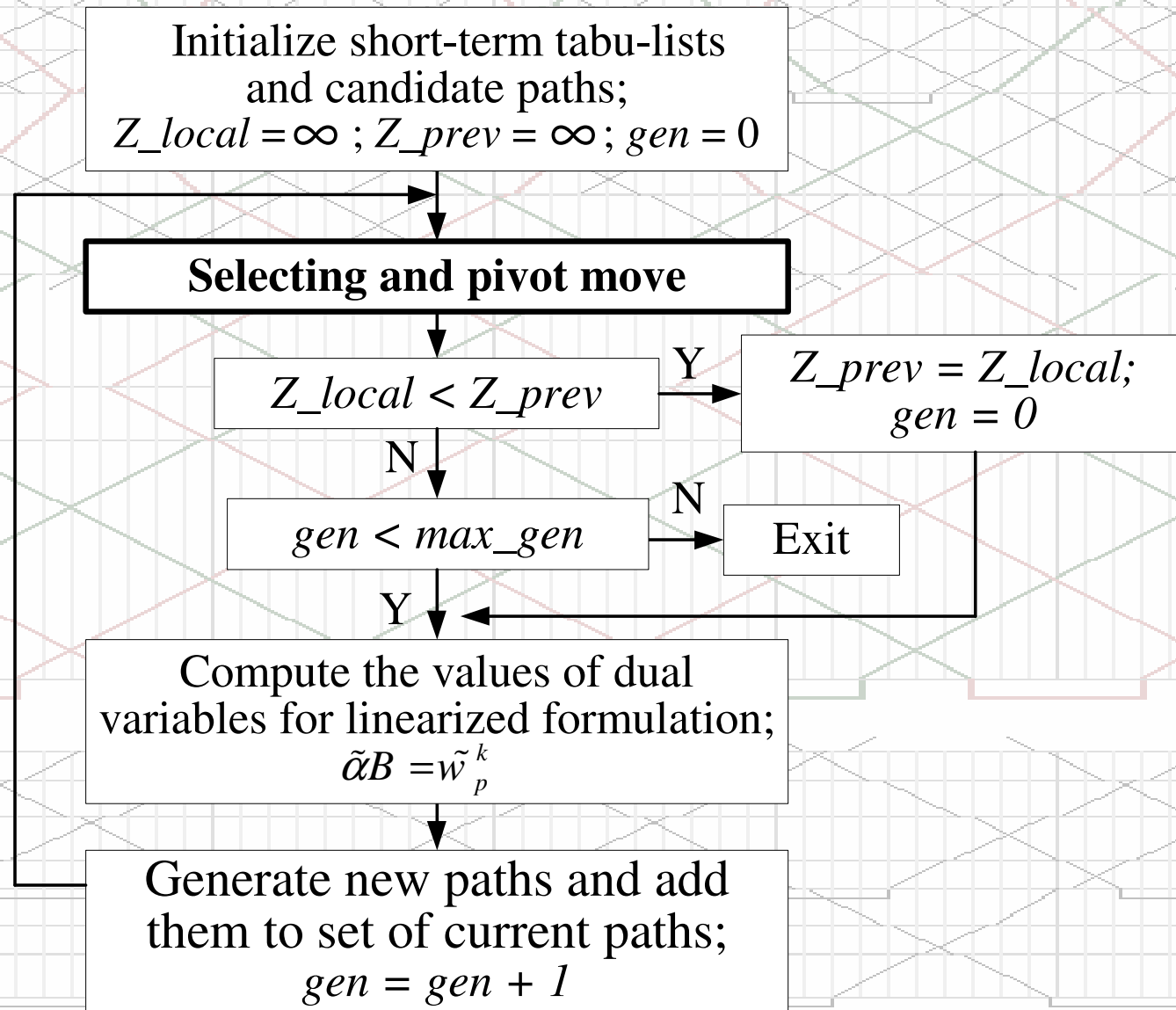
- ***div***: the number of consecutive unimproving diversification moves
- ***max\_div***: the maximum number of consecutive unimproving diversification moves



# Proposed Tabu Search Method

- ***tabu\_cycle***: the trains and paths which are closed at diversification move are tabu for *tabu\_cycle* column generation cycles
- ***sr\_close***: percentage of train services which are closed at each diversification

# Local Search – Column Generation Cycle



# Local Search – Column Generation Cycle

- ***Short-term tabu list***: path variables that recently got out the basis
- ***tabu\_tenure***: the number of iteration which an exiting variable remain in short-term tabu list

# Local Search – Column Generation Cycle

- ***gen***: the number of consecutive unimproving column generation cycles
- ***max\_gen***: the maximum number of consecutive unimproving column generation cycles
- ***pa\_gen***: the number of paths generate for each commodity during the column generation cycle

# Local Search – Column Generation Cycle

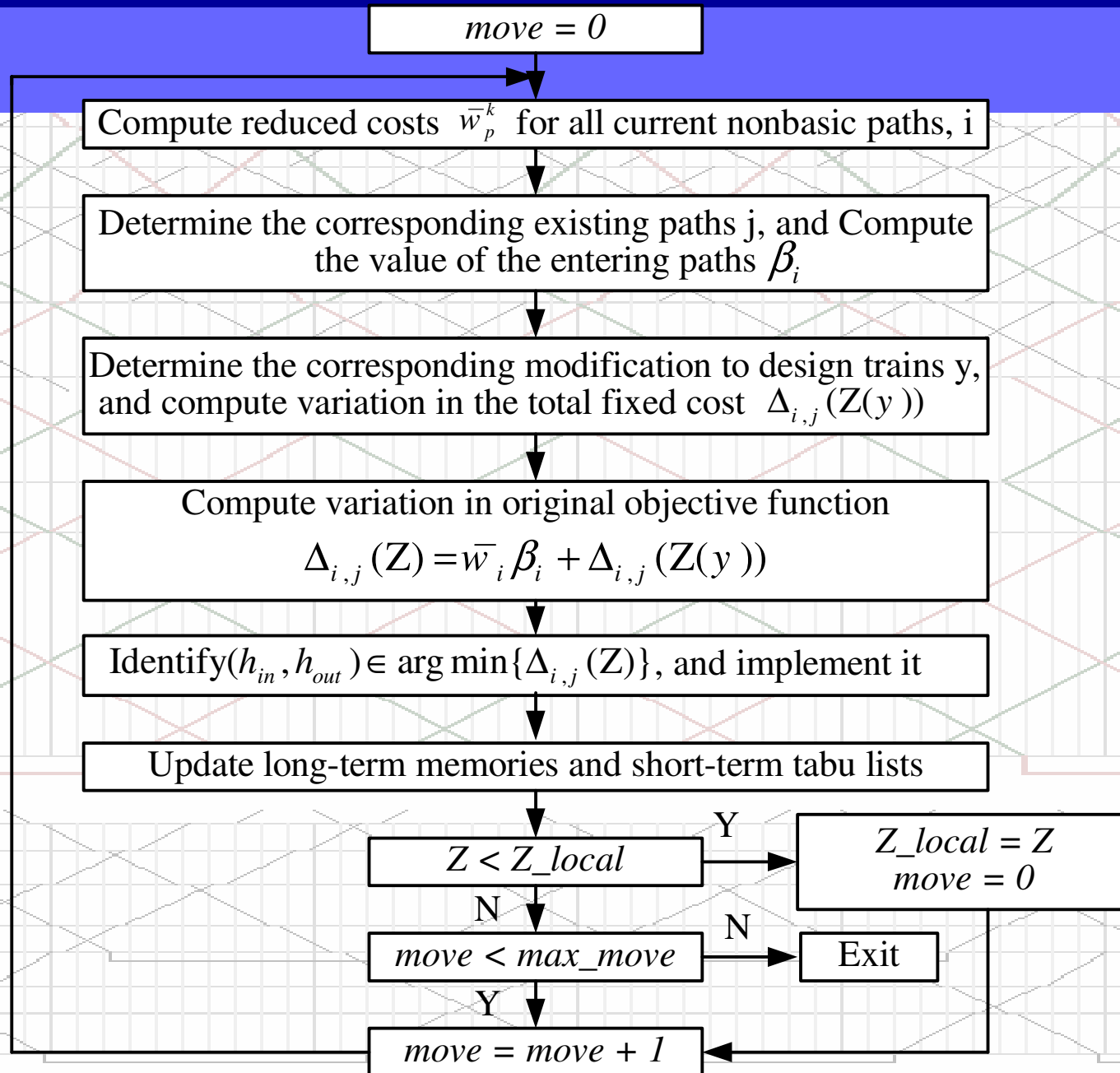
Linearized formulation:

$$z(\tilde{h}_p^k) = \sum_{k \in K} \sum_{p \in P^k} \tilde{w}_p^k h_p^k$$

where

$$\tilde{w}_p^k = w_p^k + \sum_{s \in S} \delta_{sl}^{pk} (f_s / u_s)$$

# Selecting and Pivot Moves



# Selecting and Pivot Moves

- ***move***: the number of consecutive unimproving revised simplex method moves
- ***max\_move***: the maximum number of consecutive unimproving revised simplex method moves

# Input Data

- Network
- Freight Trains
- Demands



# Input Data

## ➤ Network

- **Capacity of each track section for freight trains**
- **Number of cars which can be stored at each yard**
- **Number of trains which can be made up and broken up at each yard**
- **Average cost of set off and pick up operation per car at each yard**

# Input Data

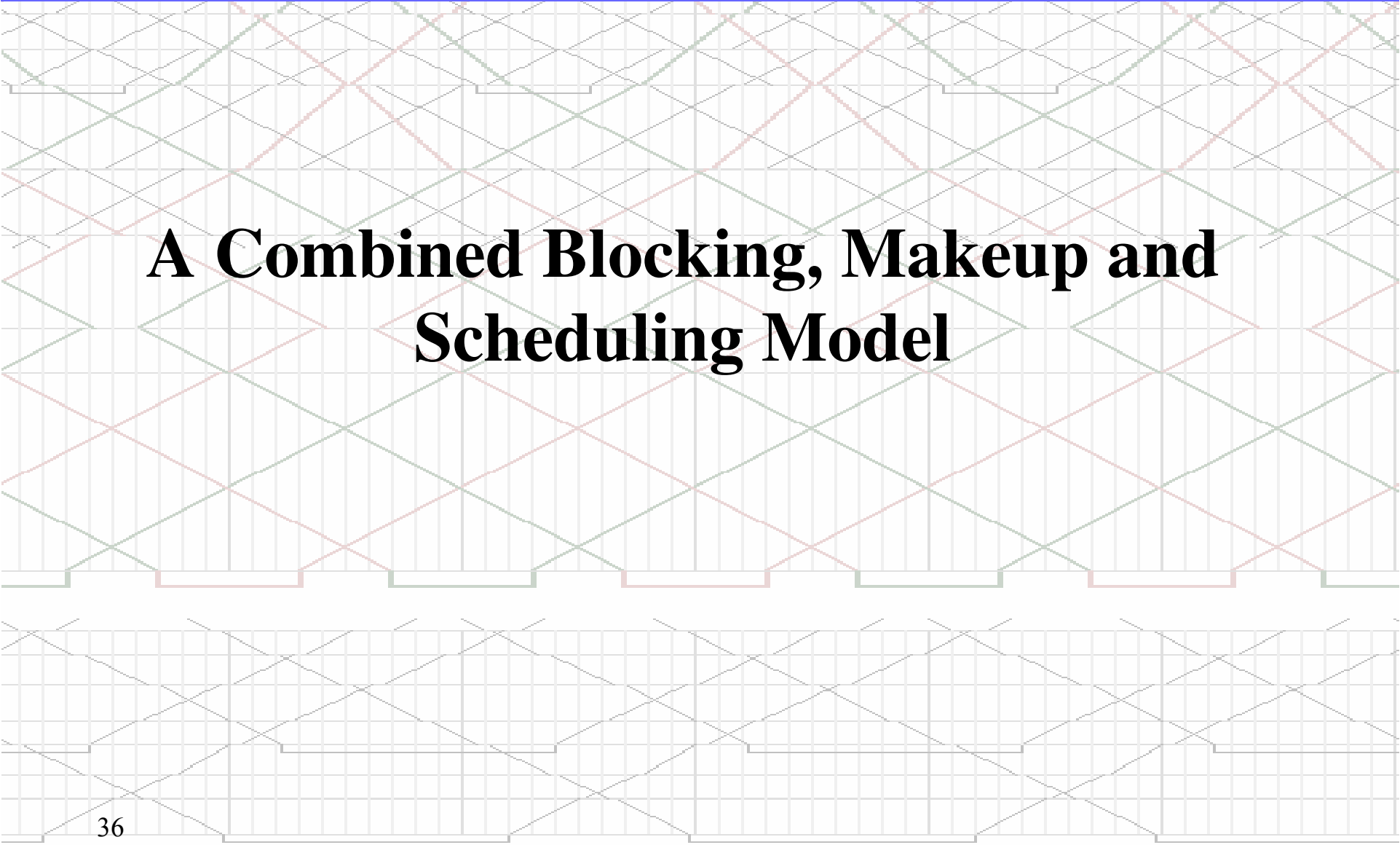
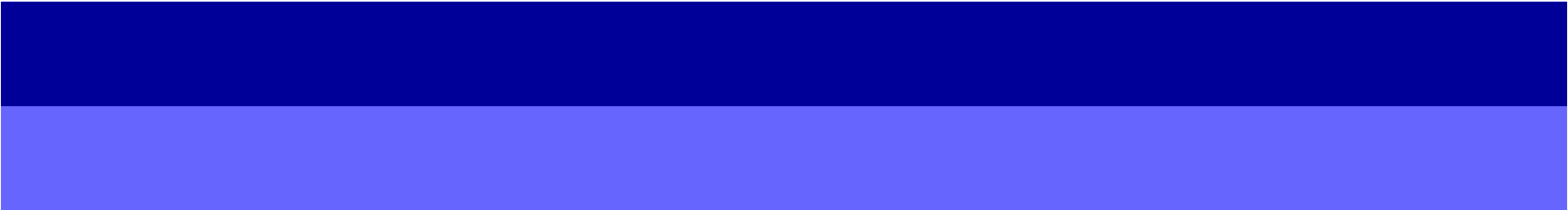
## ➤ Freight Trains

- **Types of freight trains**
- **Origin and destination of freight trains**
- **Running time between yards**
- **Intermediate stops and operations (set off or pick up)**
- **Train capacity (number of cars)**
- **Fixed cost of running of the freight trains**
- **Number of locomotive and their cost for each train**
- **Variable cost per car**

# Input Data

## ➤ Demands

- **Origin and destinations of demands**
- **Volume and type of each demand**
- **Arrival time of each demand at the origin station**
- **Maximum transport time for each demand (if there is**



# **A Combined Blocking, Makeup and Scheduling Model**