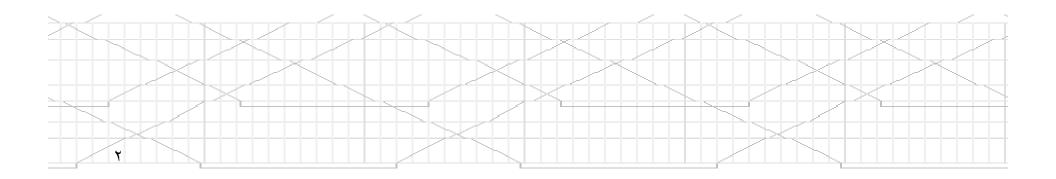
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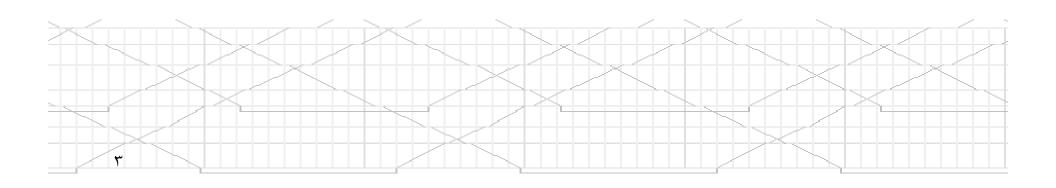


LINGO Software Overview



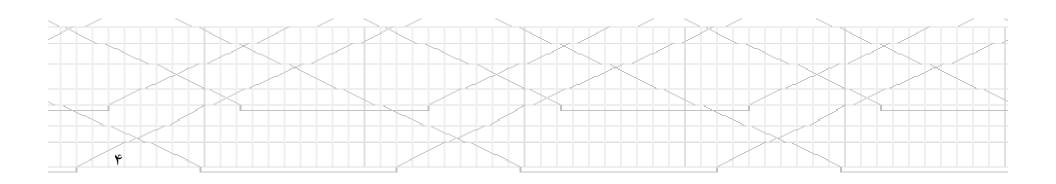
Optimization Software

- Spreadsheet (e.g, MS Excel)
 - Solver (Optimizers) (e.g., LINDO, CPLEX)
- Modeling Language (e.g., GAMS)
- Combination of Modeling Language and Solver (e.g., *LINGO*)



LINGO Software Overview

- LINGO is a software tool designed to efficiently build and solve optimization models
 - Linear programs
 - Nonlinear programs
 - Integer programs



LINGO Software Overview

- It lets you express your problem in a natural manner which is very similar to standard mathematical notation.
- Instead of entering each term of each constraint explicitly, you can express a whole series of similar constraints in a single compact statement .
- In LINGO, you can use set-based models which are useful for problems involving large numbers of similar variables and constraints.

An Optimization model

- An Optimization model consists of 3 parts
 - Objective Function
 - A single formula that describes exactly what the model should optimize
 - Variables
 - Quantities that can be changed to produce the optimal value of the objective function
 - Constraints
 - formulas that define the limits on the values of the
 - variables

Lingo Operators

- Addition: +
- Multiplication: *
- Subtraction: -
- Division: /
- For exponents: X^n
- Equals: =
- Greater than or less than: > or <
 - Note: Lingo accepts '<' as being '<='. It does not support strictly less than or greater than.

A Sample Model

- A cookie store can produce drop cookies and decorated cookies, which sell for \$1 and \$1.50 apiece, respectively.
- The two bakers each work 8 hours per day and can produce up to 400 drop cookies and 200 decorated cookies.
- It takes 1 minute to produce each drop cookie and 3 minutes to produce each decorated cookie.
- What combination of cookies produced will maximize the baker's profit?

A Sample Model

! Cookie Store Model ;

MAX = 1*Drop + 1.5*Deco;

Drop <= 400; Deco <= 200;

• Lingo Model:

1/60*Drop + 3/60*Deco <=16;

Things to notice

- Comments in the model are initiated with an exclamation point (!) and appear in green text
- Enter the objective function by typing:
 - MIN= ...; or MAX= ...;

- ST

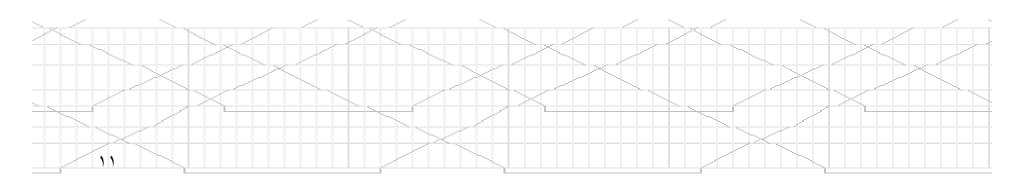
– SUCH THAT

– SUBJECT TO

• Start the constraints immediately after the objective, without:

Things to notice

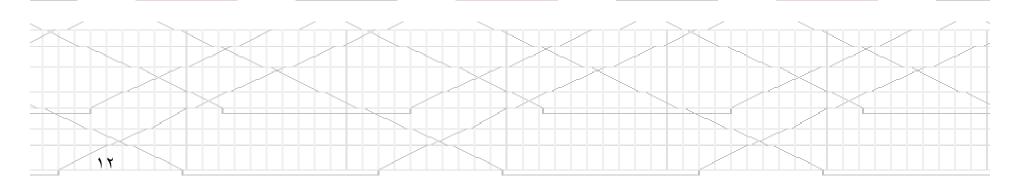
- LINGO specified operators and functions appear in blue text
- All other text is shown in black
- Each LINGO statement must end in a semicolon (;)
- Variable names are not case-sensitive and must begin with a letter (A-Z)



Solving a LINGO Model

- Once the model has been entered into the *Model Window*, it can be solved by:
 - clicking the Solve button
 - Selecting Solve from the LINGO menu
 - Using the ctrl+s keyboard shortcut

• Errors (if any) will be reported



LINGO Solver Status Window

Variables

Total

2 0 0

4 Ο.

б. 0

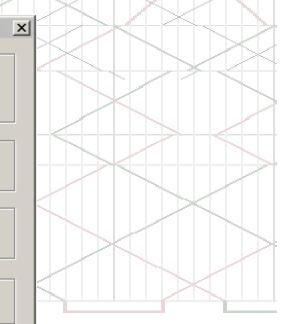
• If no errors are found, the LINGO Solver Status window appears

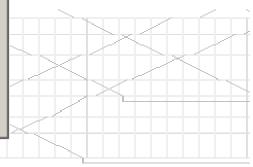
Solver Status

LINGO Solver Status [cookie_store]

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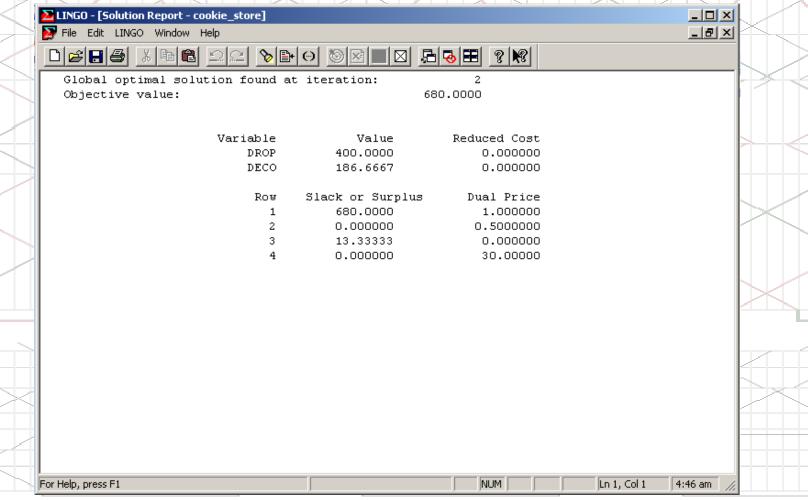
	Model Class:		I	'b	Nonlinear:
	State:	Global	Optimu	110	Integers:
	Objective:		66	0	Constraints
	Infeasibility:			0	Total:
	Iterations:			2	Nonlinear:
					Nonzeros
	-Extended Sol	ver Status-			Total:
	Solver Type				Nonlinear:
	Best Obj:				Generator Memory Used (K)
	Obj Bound:				4
	Steps:				- ⊢Elapsed Runtime (hh:mm:ss)
	Active:			•	00:00:00
	<u>U</u> pdate Interva	al: 2		Inter	rupt Solver <u>Close</u>
-					
		-			





Close the Solver Status window to see the Solution Report window

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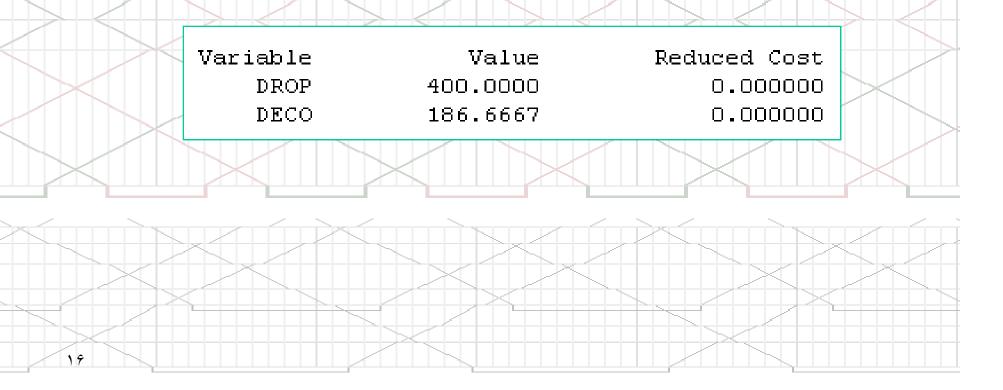


- Slack or Surplus
 - Zero: if a constraint is completely satisfied as an equality
 - Positive: shows how many more units of the variable could be added to the optimal solution before the constraint becomes an equality

Row	Slack or Surplus
1	680.0000
2	0.00000
3	13.33333
4	0.00000

Reduced Cost

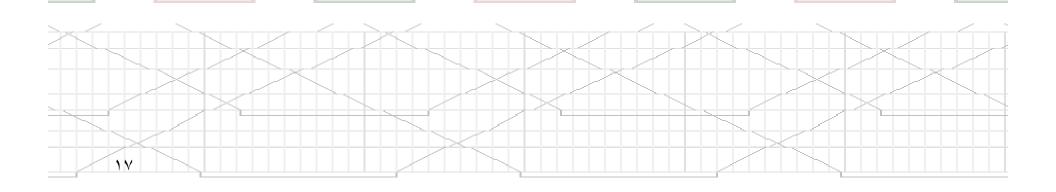
 How much the objective function would degrade if one unit of a variable (not included in the current solution) were to be included



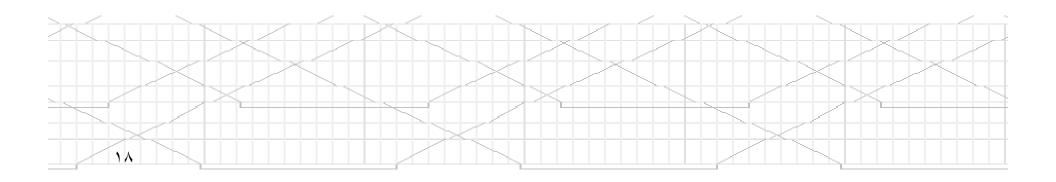
• Dual Price

- How much the objective function would improve if
 - the constraining value is increased by one unit

Row	Slack or Surplus	Dual Price
1	680.0000	1.000000
2	0.00000	0.5000000
3	13.33333	0.000000
4	0.00000	30.00000
		KNIK

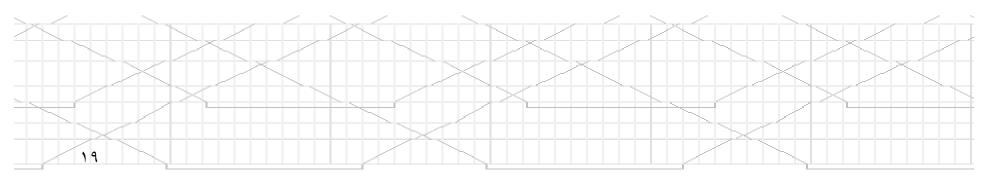


LINGO Modeling Language



Using Sets in LINGO

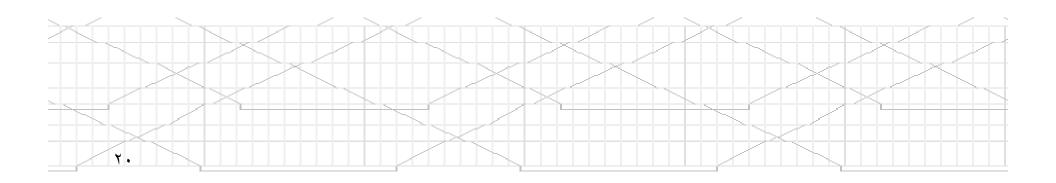
- LINGO allows you to group many instances of the same variable into sets
 - Example: If a model involved 27 delivery trucks, then these 27 trucks could be described more simply as a single set
- Sets may also include attributes for each member, such as the hauling capacity for each delivery truck



Using Sets

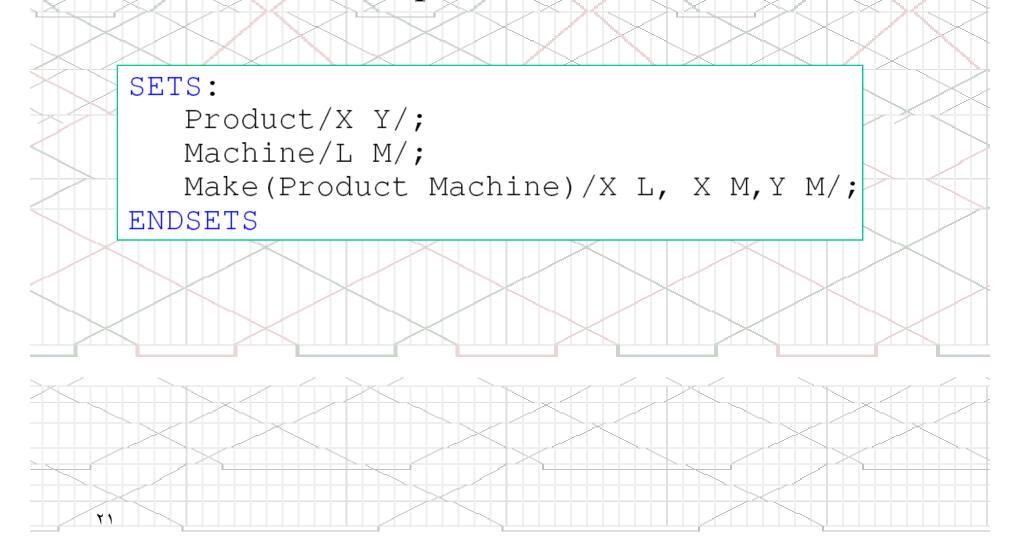
- SETS section must be defined before any of the set members are used in the model's
 - constraints
- Primitive set example:

SETS: Trucks/TR1..TR27/:Capacity; ENDSETS



Using Sets

• Derived set example:



Set Looping Statement Examples

@FOR(Trucks(T): Capacity(T)<=3000);</pre>

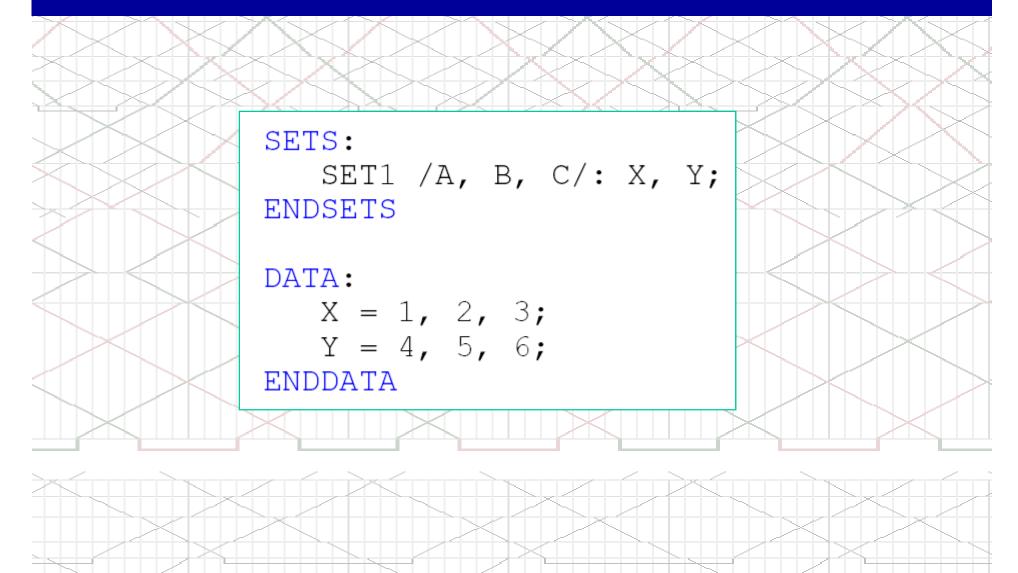
 This @FOR statement sets the hauling capacity for all 27 delivery trucks in the Trucks set to at most 3000 pounds

TOTAL_HAUL=@SUM(Trucks(J): Capacity(J));

This @SUM statement calculates the total

hauling capacity from the individual trucks

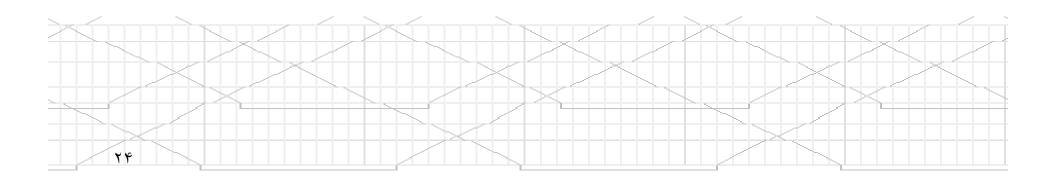
LINGO Data Example



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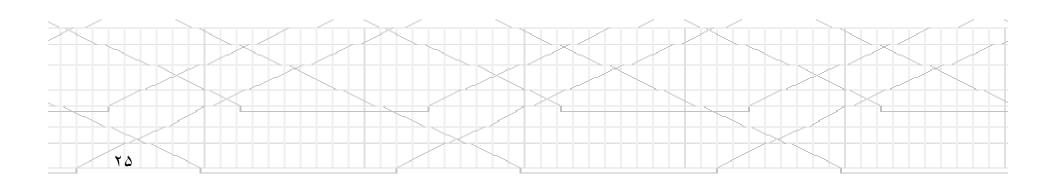
Variable Types in LINGO

- All variables in a LINGO model are considered to be non-negative and continuous unless otherwise specified
- LINGO's four variable domain functions can be used to override the default domain for given variables



Variable Types in LINGO

- @GIN any positive integer value
- @BIN a binary value (ie. 0 or 1)
- @FREE any positive or negative real value
- @BND any value within the specified bounds



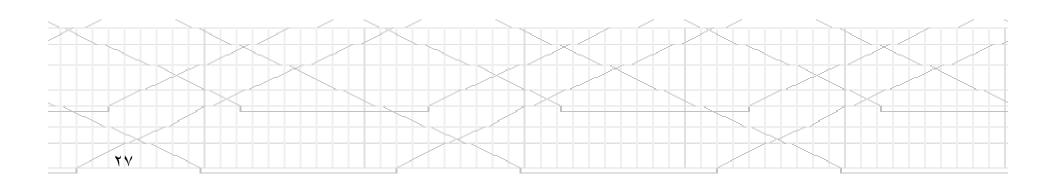
Mathematical Functions

- @ABS(X) returns the absolute value of X
- @SIGN(X) returns -1 if X is negative and +1 if X is positive
- @EXP(X) –calculates e^X
 - @LOG(X) calculates the natural log of X
- @SIN(X) returns the sine of X, where X is the angle in radians
- @COS(X) returns the cosine of X

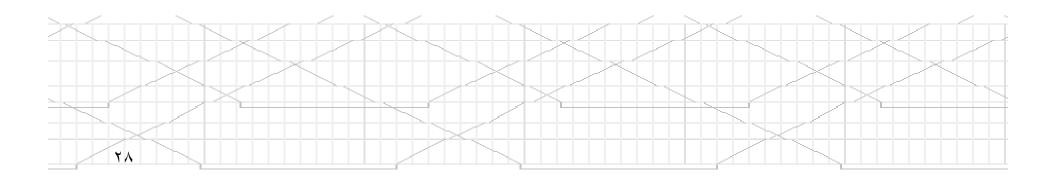
• @TAN(X) – returns the tangent of returns the tangent of X

Other Functions in LINGO

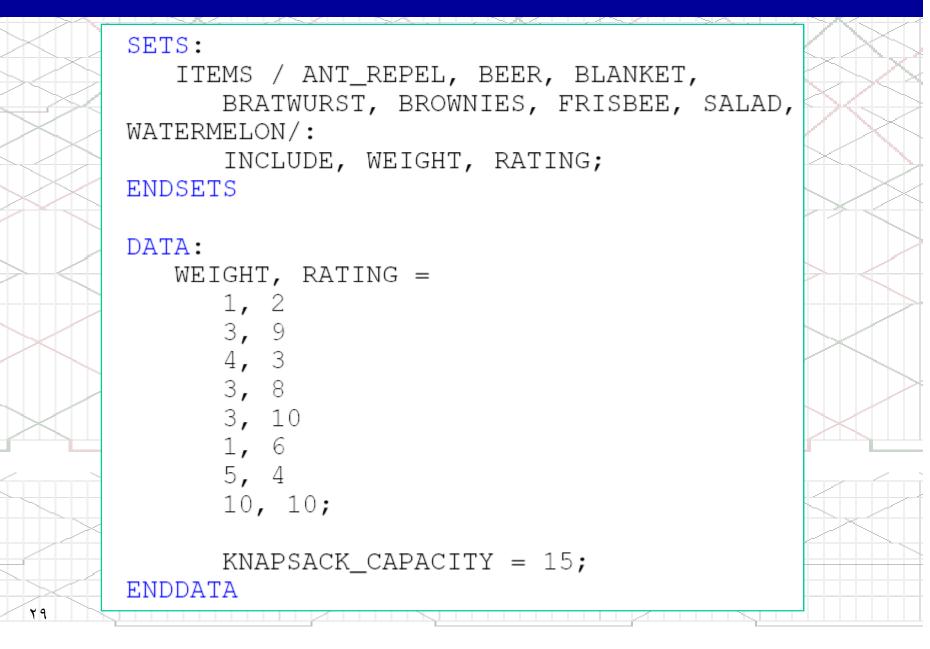
- LINGO also contains a lot of financial, probability, and import/export functions
- These are commonly used in more advanced
 - models



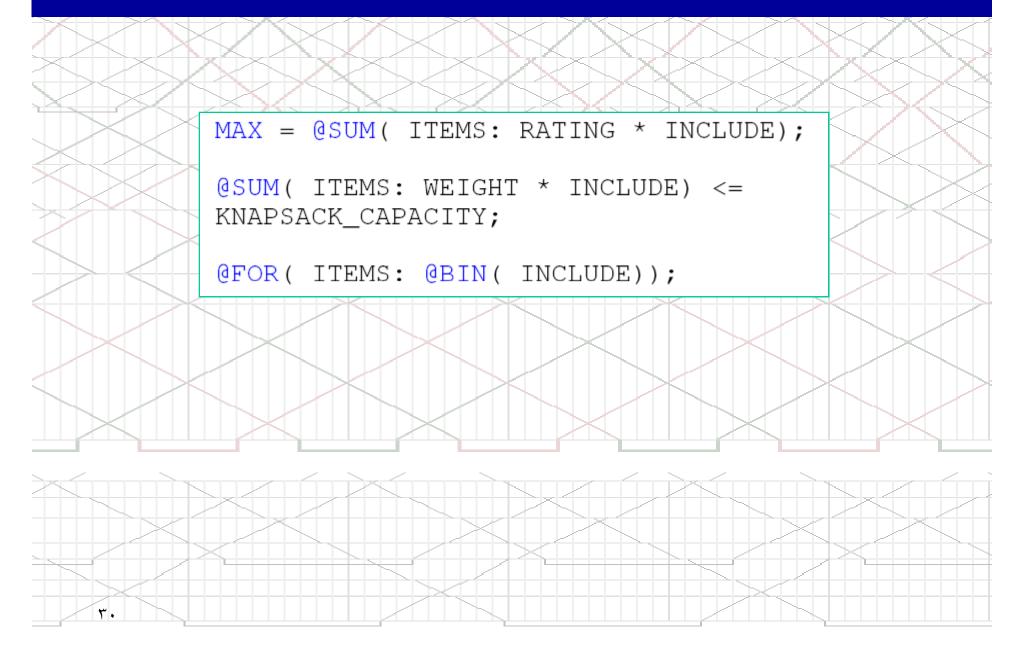
Example I: Knapsack Problem



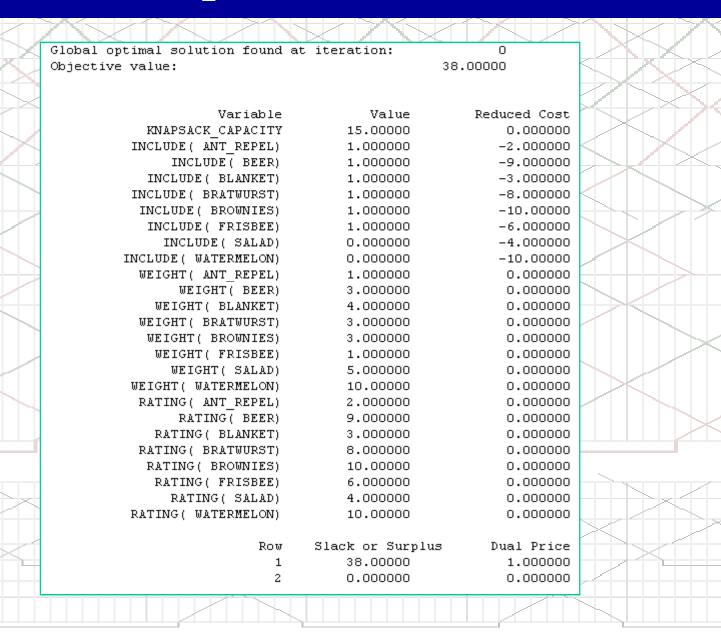
Knapsack Problem



Knapsack Problem

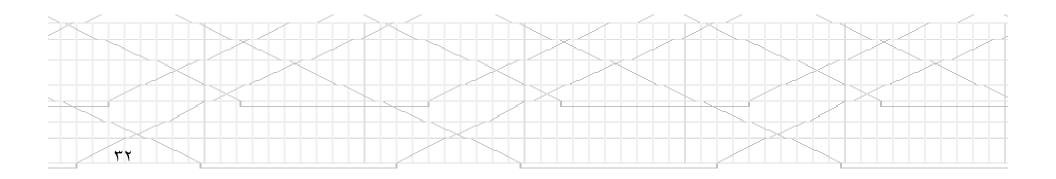


Knapsack Problem



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Example II: Bisco Problem



Bisco Problem

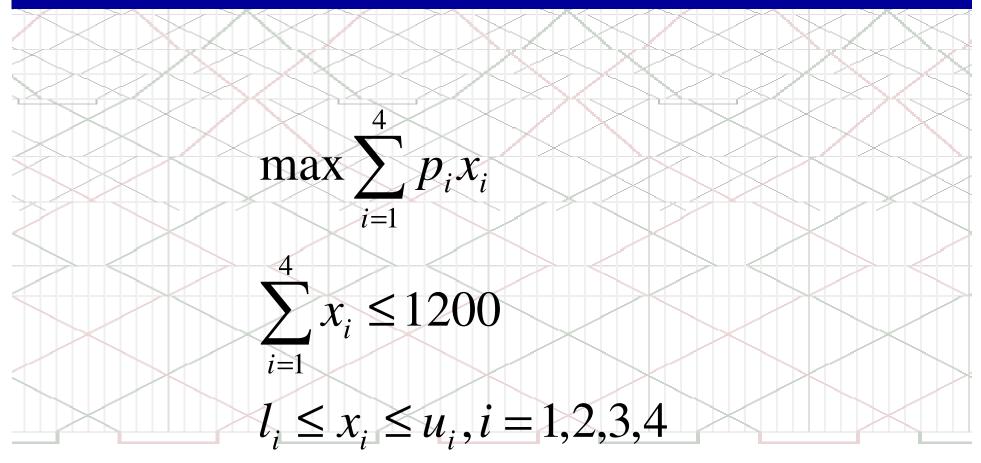
Bisco's new sugar-free, fat-free chocolate squares are so popular that the company cannot keep up with demand.
 Regional demands shown in the following table total 2000 cases per week, but Bisco can produce only 60% (1200 cases) of that number.

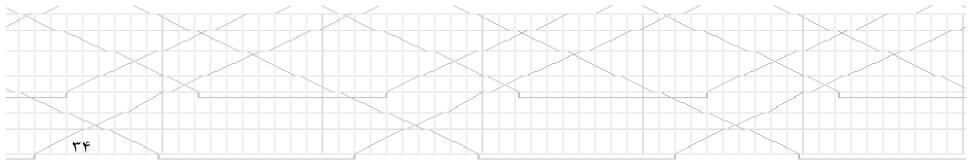
	NE	SE	MW	W
Demand	620	490	510	380
Profit	1.6	1.4	1.9	1.2

• The table also shows the different profit levels per case experienced in the regions due to competition and consumer tastes. Bisco wants to find a maximum profit plan that fulfils between 50% and 70% of each region's demand.

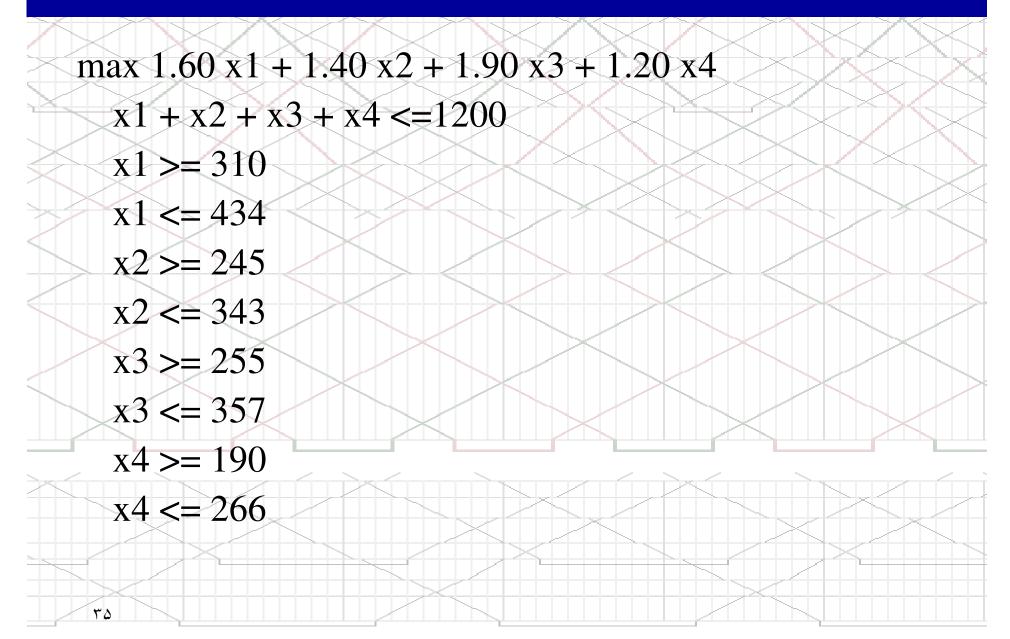
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Problem Formulation

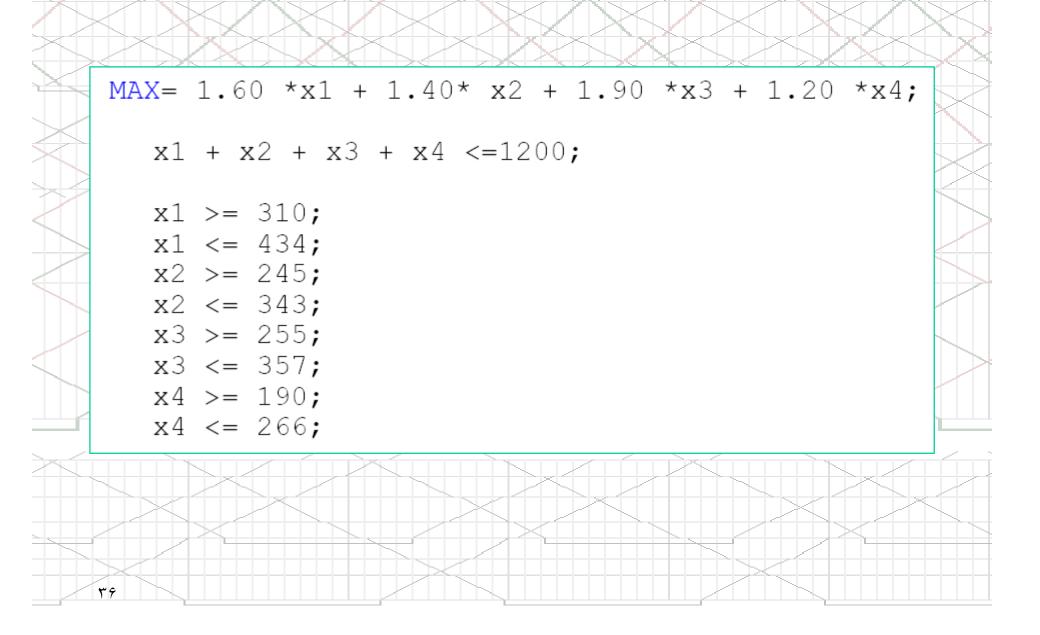




Problem Formulation



LINGO Model



LINGO Solution

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			\sim	
Objective v	alue:	19	02.100	INX/N
	Variable	Value	Reduced Cost	
	X1	408.0000	0.000000	
	X2	245.0000	0.000000	
	Х3	357.0000	0.000000	
	X4	190.0000	0.000000	
	Row	Slack or Surplus	Dual Price	
	1	1902.100	1.000000	
	2	0.000000	1.600000	
	3	98.00000	0.000000	
	4	26.00000	0.000000	
	5	0.000000	-0.2000000	
	6	98.00000	0.00000	
	7	102.0000	0.000000	
	8	0.00000	0.300000	
	9	0.000000	-0.4000000	
	10	76.00000	0.000000	
<u> </u>				

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LINGO Model 2

```
SETS:
   REGIONS / NE SE MW W/: LBOUND, UBOUND, PROFIT, CASES;
ENDSETS
DATA:
   LBOUND = 310 245 255 190;
   UBOUND = 434 343 357 266;
   PROFIT = 1.6 1.4 1.9 1.2;
ENDDATA
MAX = (SUM(REGIONS(I): PROFIT(I)*CASES(I));
@SUM(REGIONS(I): CASES(I)) <=1200;</pre>
@FOR(REGIONS(I): CASES(I) <= UBOUND(I));</pre>
(FOR(REGIONS(I): CASES(I) >= LBOUND(I));
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```

LINGO Solution

\geq	Objective value:		1	.902.100	
					$f \times f$
4					$X \propto$
		Variable	Value	Reduced Cost	
/		LBOUND (NE)	310.0000	0.00000	
\sim		LBOUND (SE)	245.0000	0.000000	
		LBOUND (MW)	255.0000	0.000000	
		LBOUND (W)	190.0000	0.000000	
		UBOUND (NE)	434.0000	0.000000	
_		UBOUND (SE)	343.0000	0.000000	
		UBOUND (MW)	357.0000	0.000000	
\leq		UBOUND (W)	266.0000	0.000000	\times
		PROFIT(NE)	1.600000	0.000000	
		PROFIT(SE)	1.400000	0.000000	
\leq		PROFIT(MW)	1.900000	0.000000	
		PROFIT(W)	1.200000	0.000000	
		CASES(NE)	408.0000	0.000000	
		CASES(SE)	245.0000	0.000000	
/		CASES(MW)	357.0000	0.000000	
\sim		CASES(W)	190.0000	0.000000	
		Row	Slack or Surplus	Dual Price	
		1	1902.100	1.000000	
		2	0.000000	1.600000	
$\overline{\}$		3	26.00000	0.000000	NT
		4	98.00000	0.000000	
_		5	0.000000	0.3000000	
~		6	76.00000	0.000000	뭐나
4		7	98.00000	0.000000	- AL
		8	0.000000	-0.2000000	
		9	102.0000	0.000000	
		10	0.000000	-0.4000000	

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